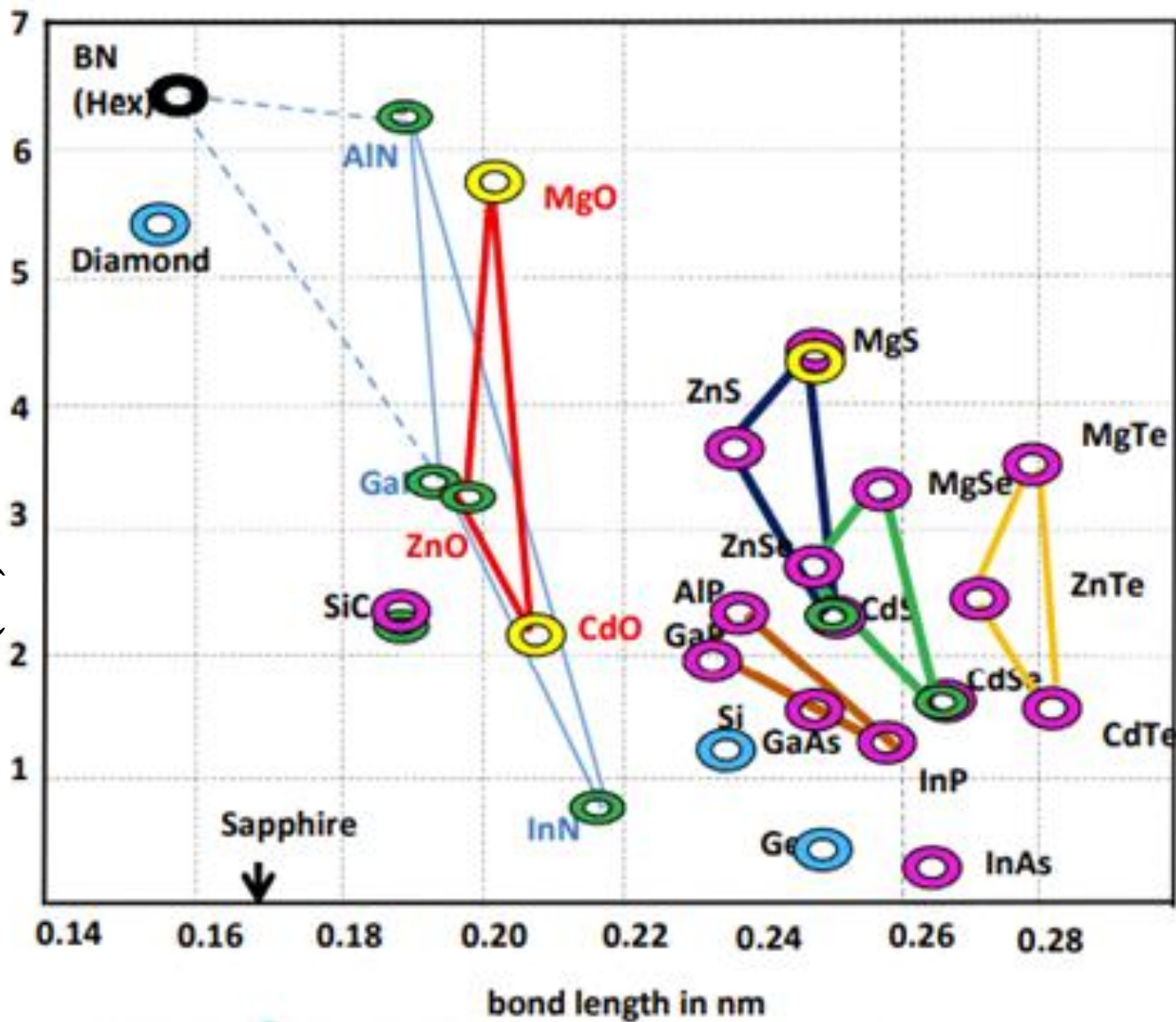


Nitrides and other semiconductors

Jean-Yves DUBOZ
CRHEA CNRS
Valbonne, France



Gap energy
(eV)



Main industrial
semiconductors

- 1-Si
 - 2-Ge
 - 3-SiC
 - 4-GaN
 - 4-GaAs
 - 5-InP
 - 6-InAs
 - 7-GaSb
 - 8-CdTe
 - 9-HgCdTe
- IV
- III-V
- II-VI

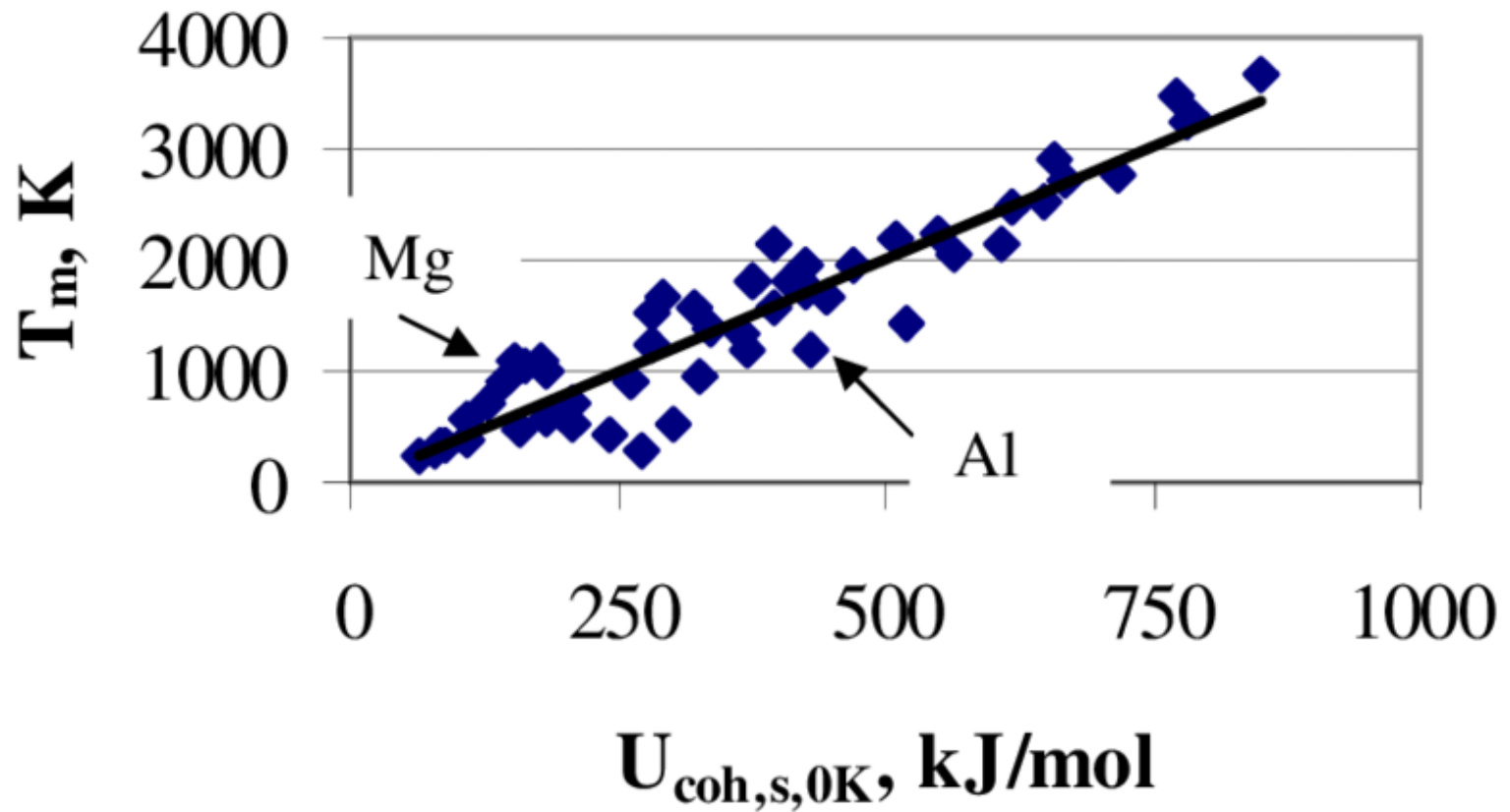
	GaN	AlN	InN	GaAs	Si	Diamond
Bond length (Å)	1.95	1.90	2.15	2.44	2.34	1.54
Bond energy (eV)	8.9*	11.5	7.7	6.5	4.7	7.4
Cohesive energy (eV/atom)	2.24	2.88	1.93	1.63	2.32	4.62
Melting point (K)	2791	3487	2146	1513	1687	3770

* About 10 meV less for the cubic phase: less stable from thermodynamics

Thermal stability
Chemical inertness
Radiation hardness



Melting temperature and cohesive energy



Ionic/covalent bond

Bond character depends
on atom electronegativity

For instance for group V elements :
 $X_N \gg X_P \gg X_{As} \gg X_{Sb}$

Bonds in nitrides are more
ionic than in many other SC

How does the validity of
tight binding methods vary
along this table ?

	Ionicity
Si	0
C (diamond)	0
AlAs	0.274
AlP	0.307
GaAs	0.310
GaP	0.327
InAs	0.357
InP	0.421
AlN	0.449
GaN	0.500
InN	0.558
NaCl	0.9

Polarization in heterostructures

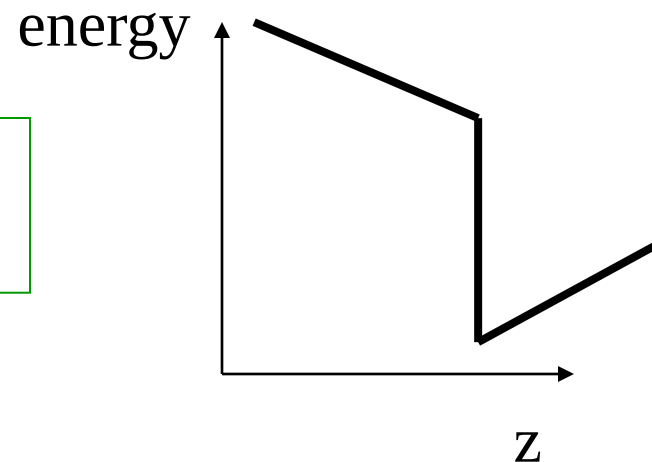
What is important is the differences in polarization between two materials (the absolute value may even not be defined (C. van de Waal))

$$E(z) = -\frac{1}{\epsilon_0 \epsilon_r} P(z)$$

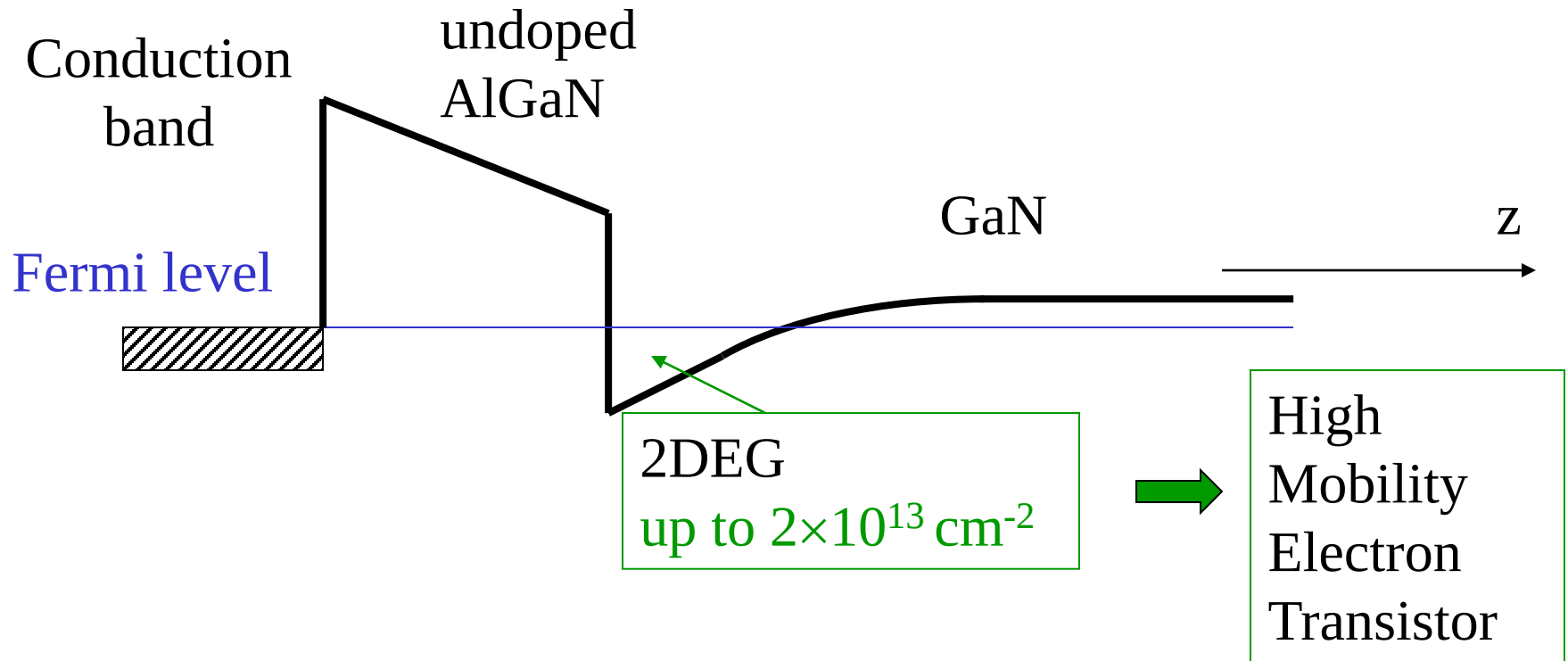
$$\Delta P = P_{\text{AlN}} - P_{\text{GaN}} \approx 0.05\text{-}0.1 \text{ C/m}^2$$

$$\Delta E = E_{\text{AlN}} - E_{\text{GaN}} \approx \Delta P / \epsilon_0 \epsilon_r \approx 6\text{-}12 \text{ MV/cm}$$

Enormous internal field
discontinuity at the interface !

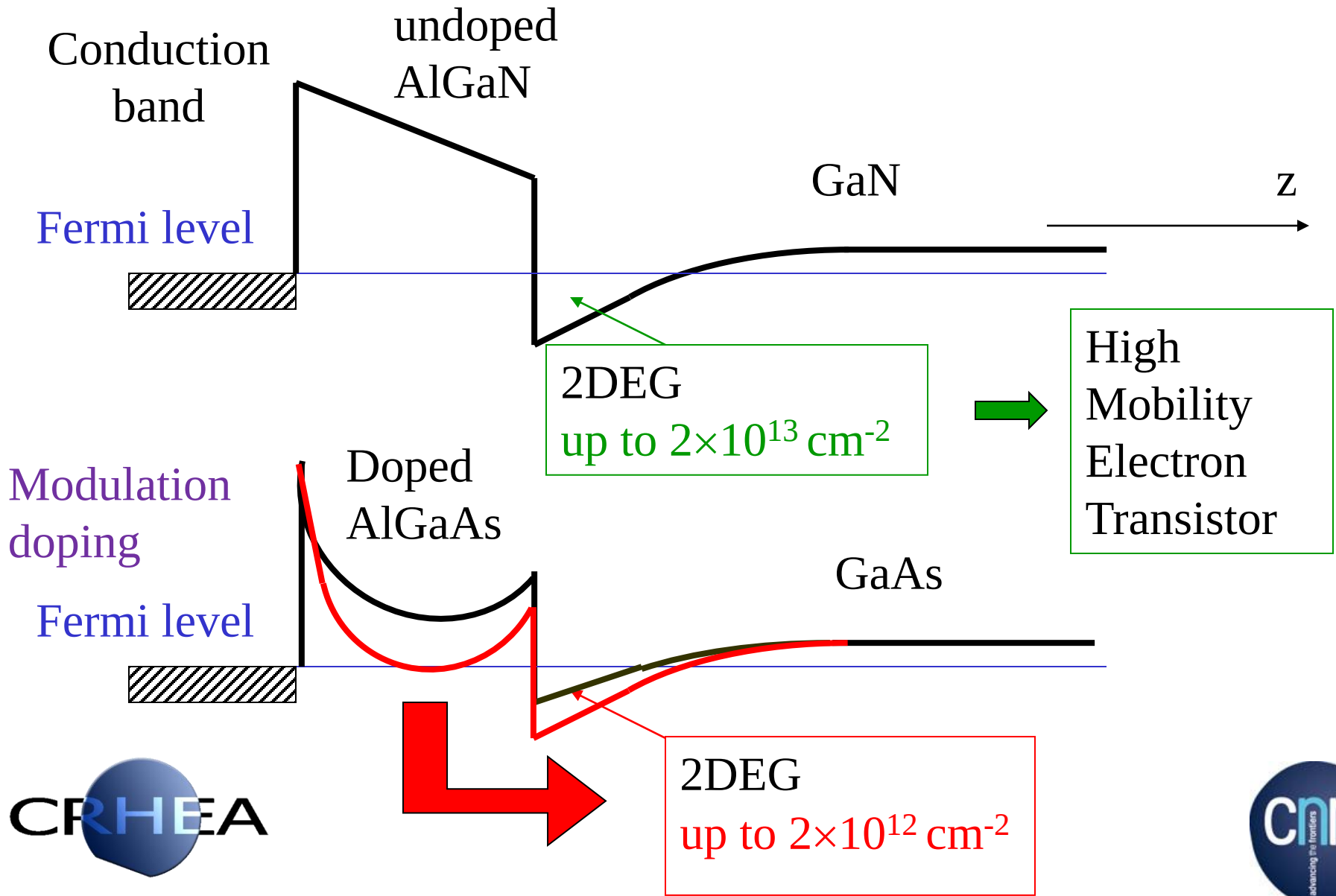


Polarization in wurzite nitrides



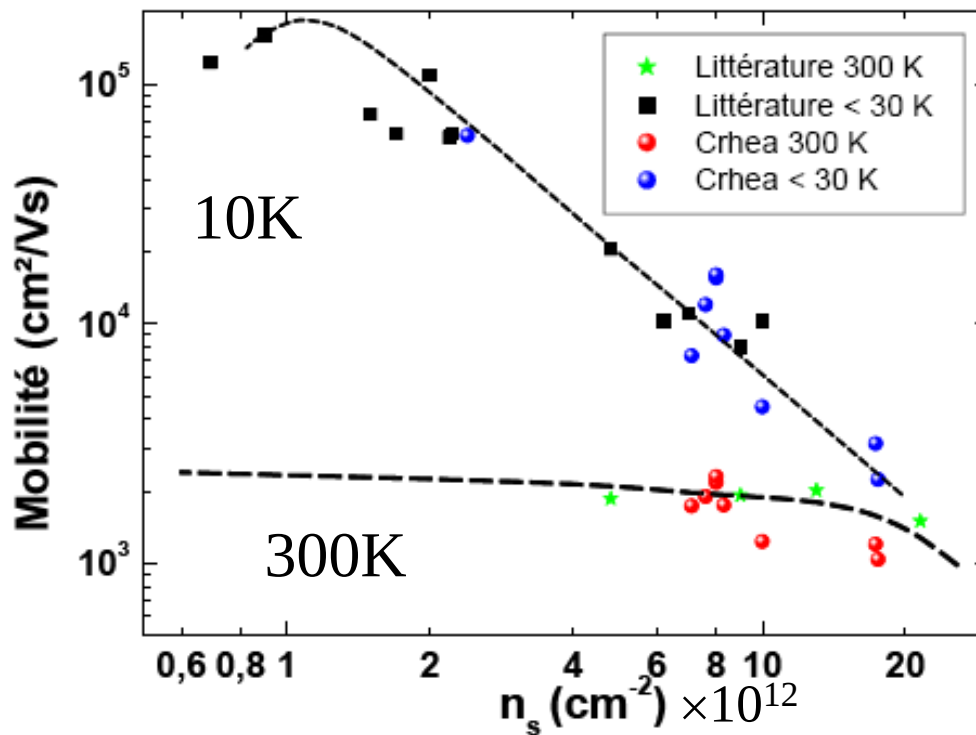
Can you get 2D gases without polarization field ?

Polarization in wurzite nitrides



Best of - GaN 2DEG

	n_s (10^{12}cm^{-2})
GaN/AlGaN	36
GaN/AlInN	42
GaAs/AlGaAs	2
InGaAs/AlInAs	8.5

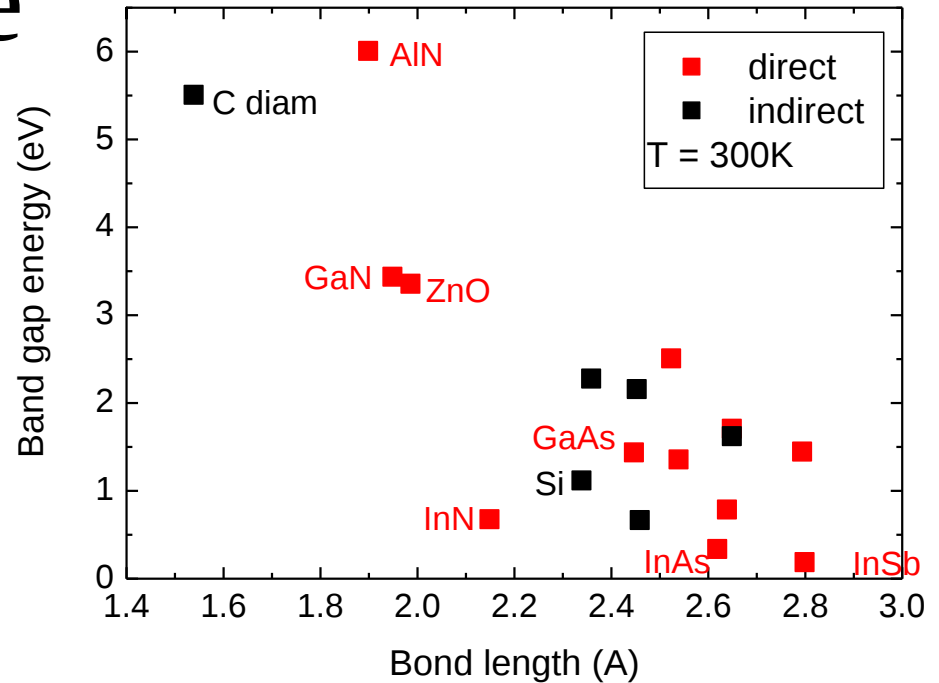


	$\mu(300\text{K})$ cm^2/Vs	$n_s(300\text{K})$ cm^{-2}	$\mu(<4\text{K})$ cm^2/Vs	$n_s(<4\text{K})$ cm^{-2}
GaN/AlGaN	2500	$4\text{-}6 \times 10^{12}$	10^5	2×10^{12}
GaAs/AlGaAs	10000	2×10^{11}	3×10^7	2×10^{11}

Why is μ smaller in GaN than in GaAs ?

Band structure

Small atoms, short bonds:
⇒ large band gap energy

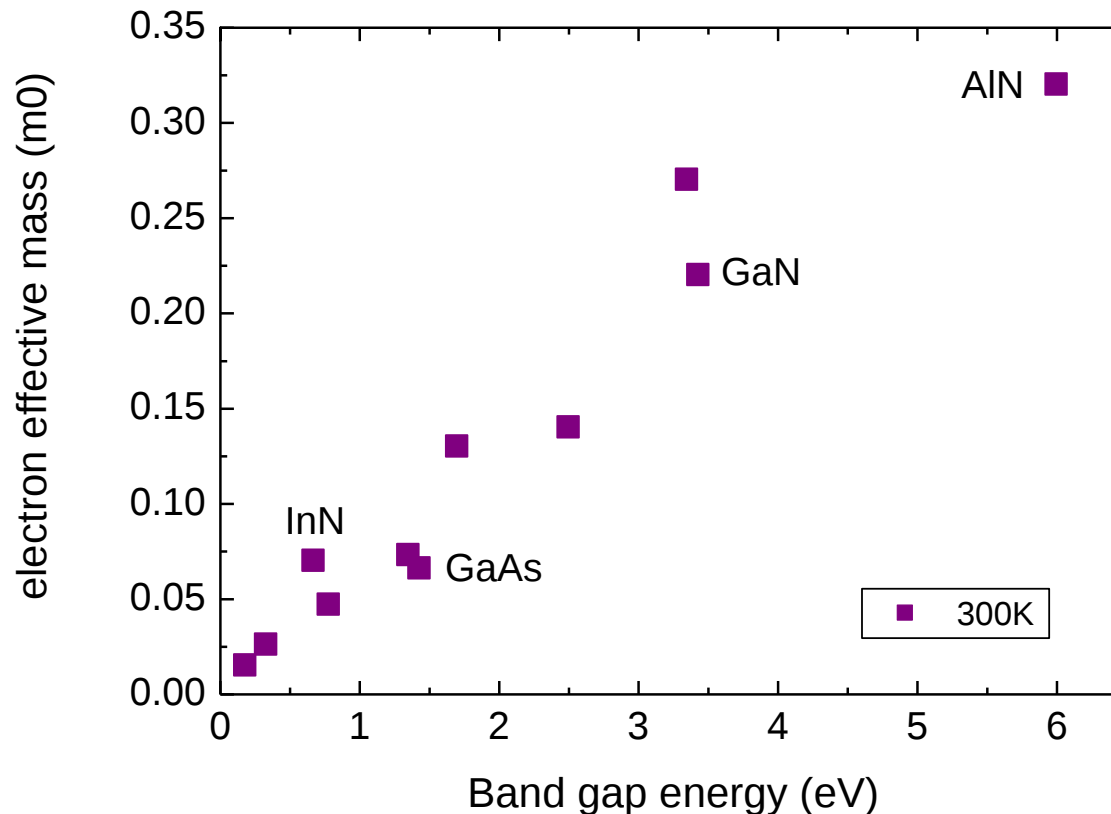


Material	c-GaN	w-GaN	AlN	InN
Band gap (300K)	3.3 eV	3.43 eV	6.0 eV	0.67 eV

All direct gap materials ! Optoelectronics from IR to UV IR:
(InN:1.85 μm) , visible (InGaN) , to UV (AlN:0.206 μm).

Band structure

Electron effective mass: follows the $m \propto E_g$ rule

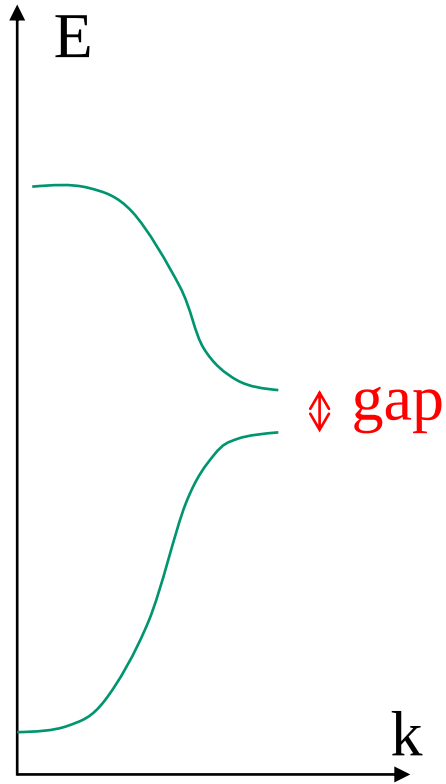


Large effective masses in nitrides

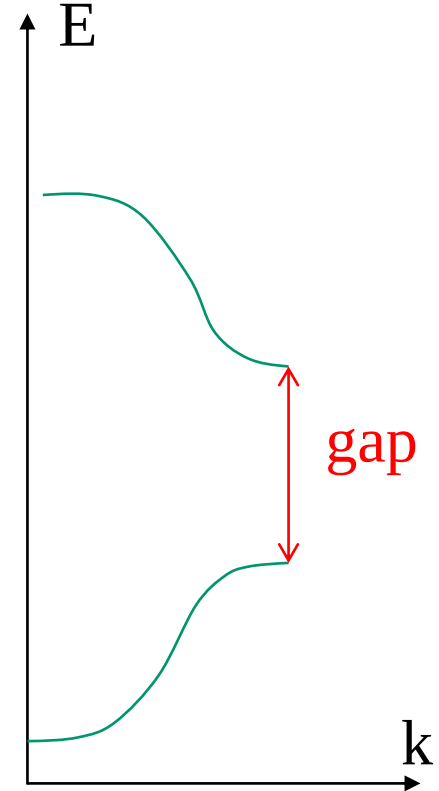
Mobilities smaller than in other III-vs

Effective mass versus band gap

$$\frac{1}{m} = \frac{\partial^2 E}{\partial k^2}$$

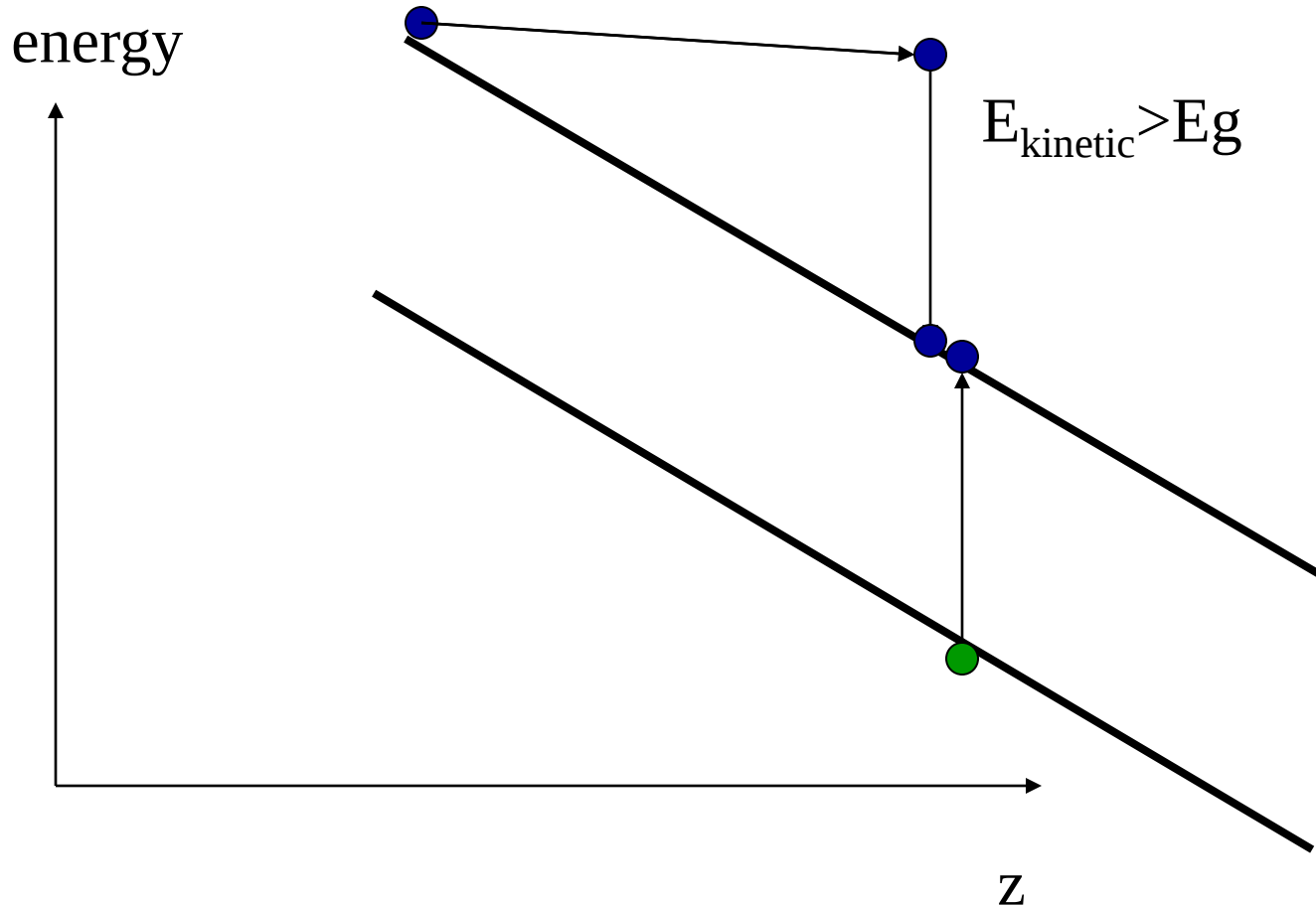


m small



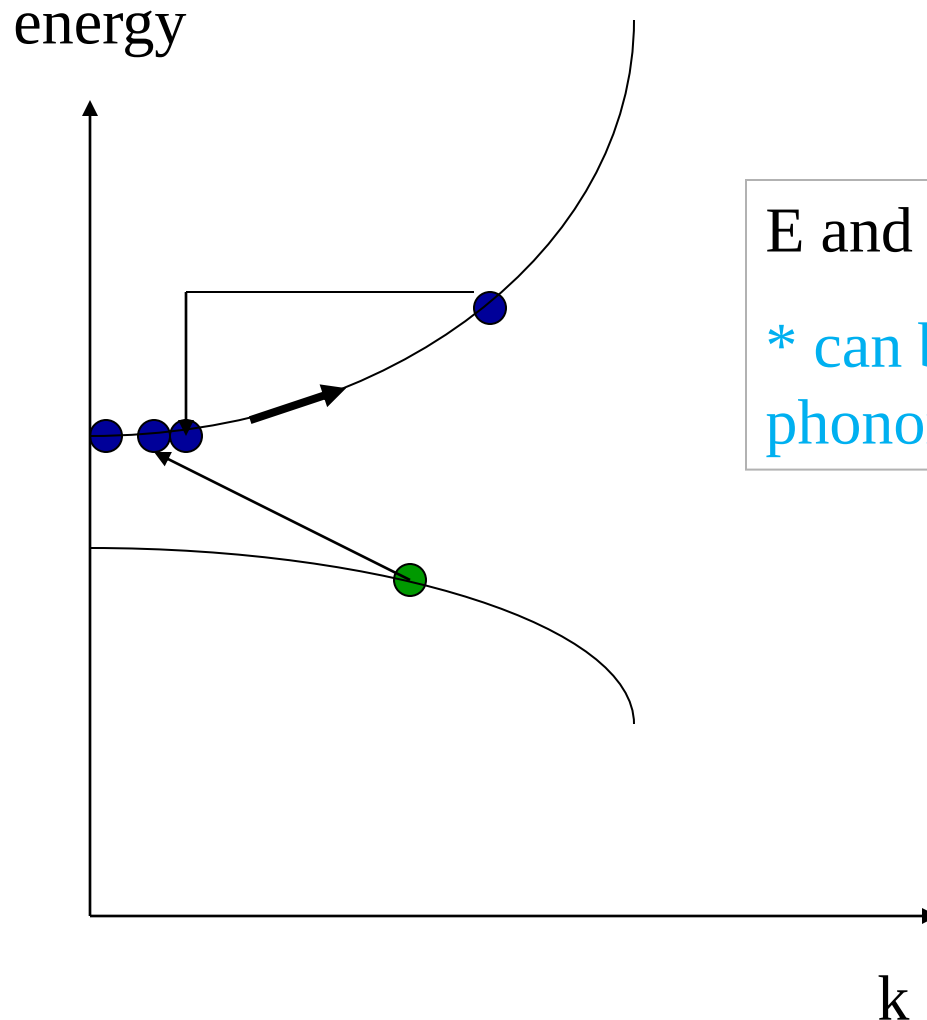
m large

Impact ionisation



On so on...avalanche breakdown
(requires a minimal thickness L so
that $\alpha L = 1!!$)

Impact ionisation

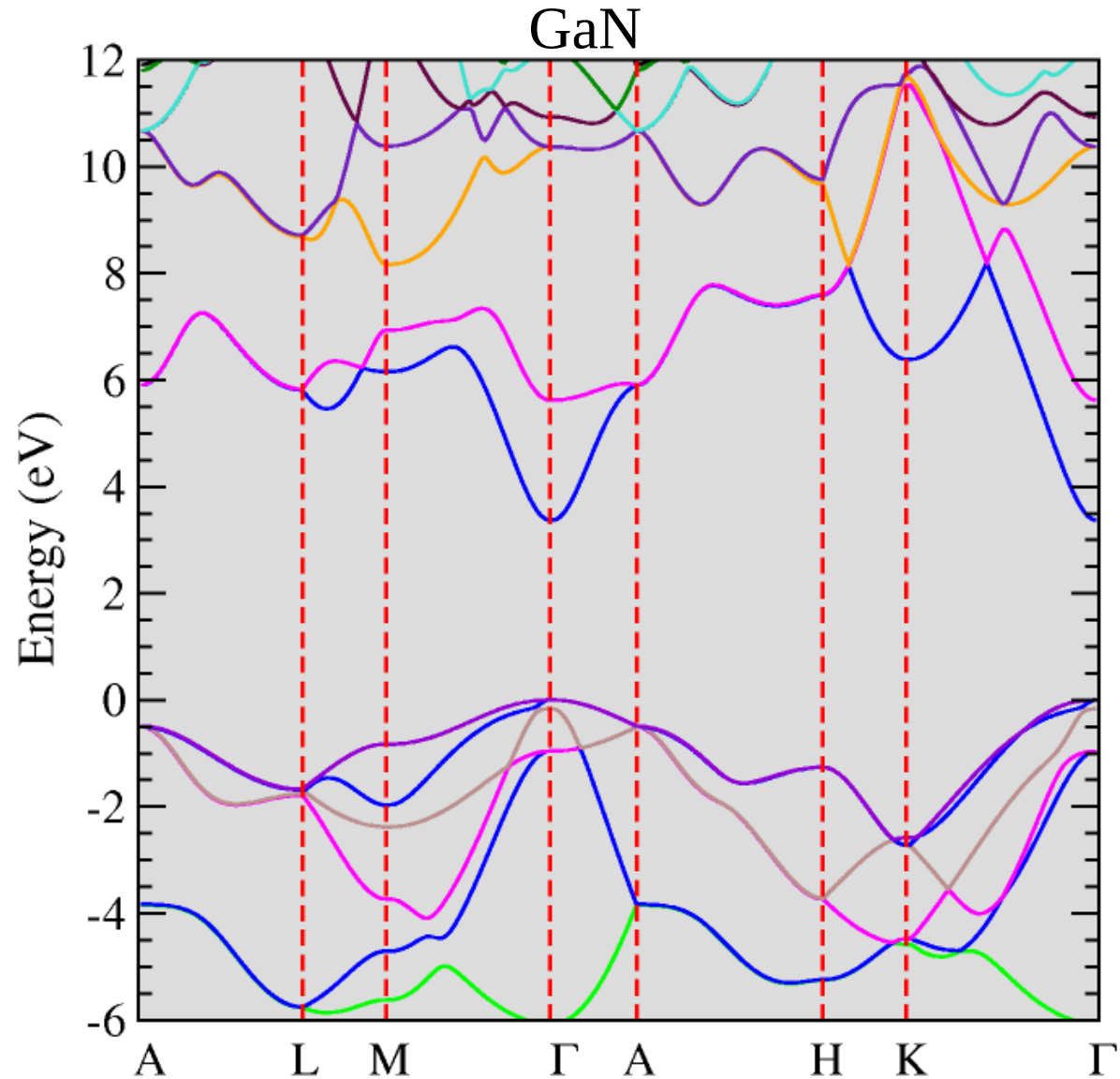


E and k conservation*

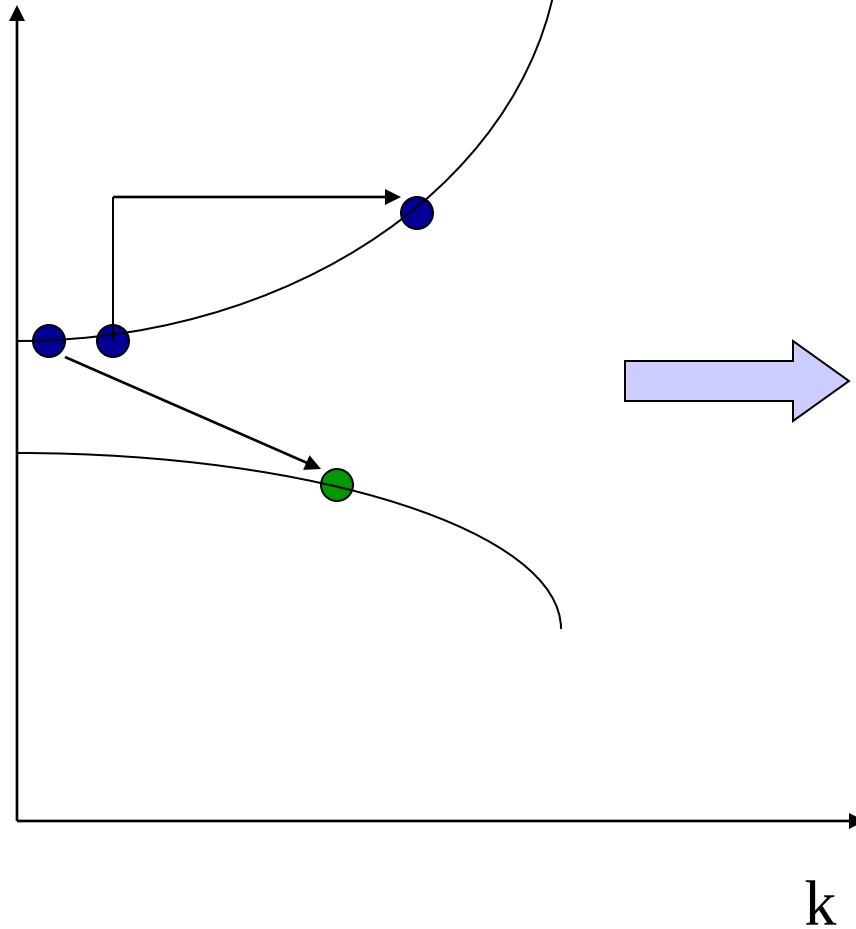
* can be relaxed if
phonon assisted

Impact ionisation

Not so easy to obey E and k conservation: ionization is weaker in wider band gap materials

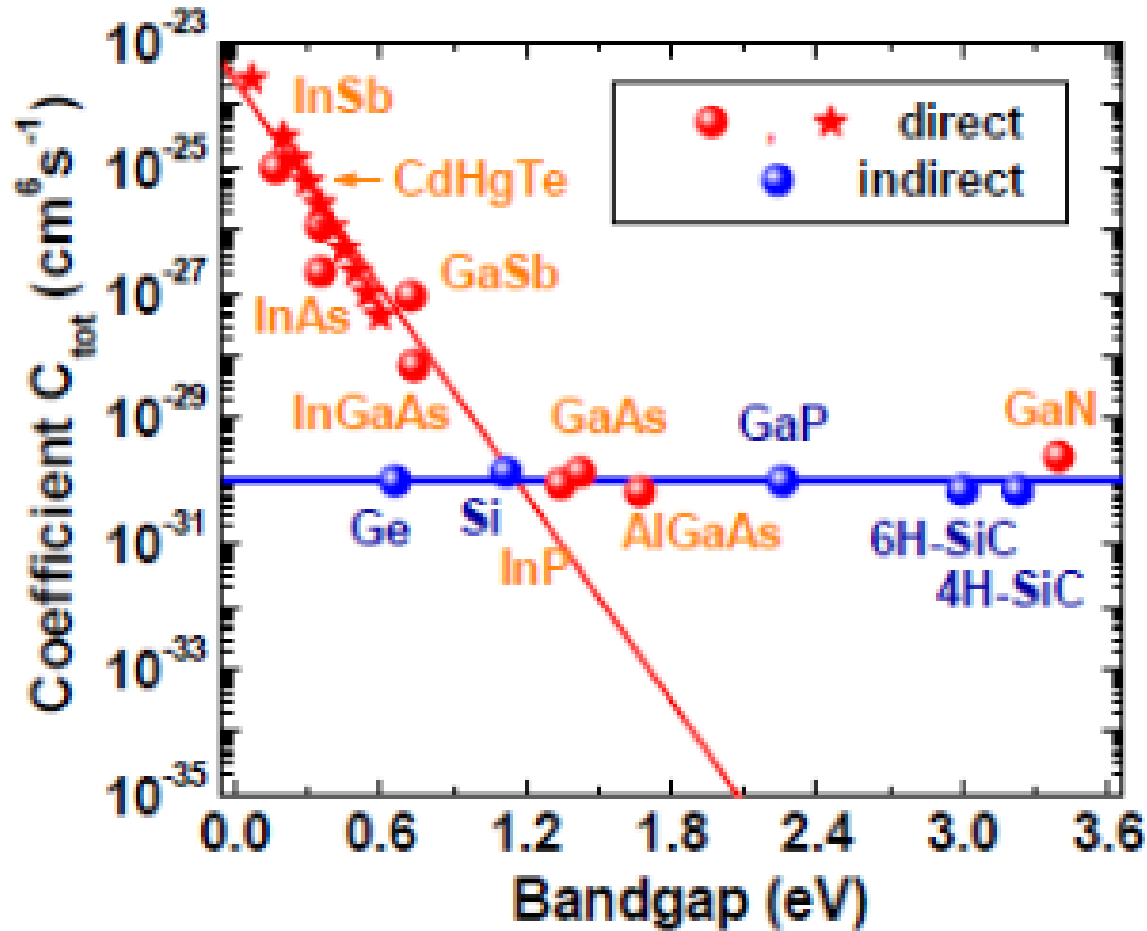


energy



Auger =
inverse
process of
impact
ionization

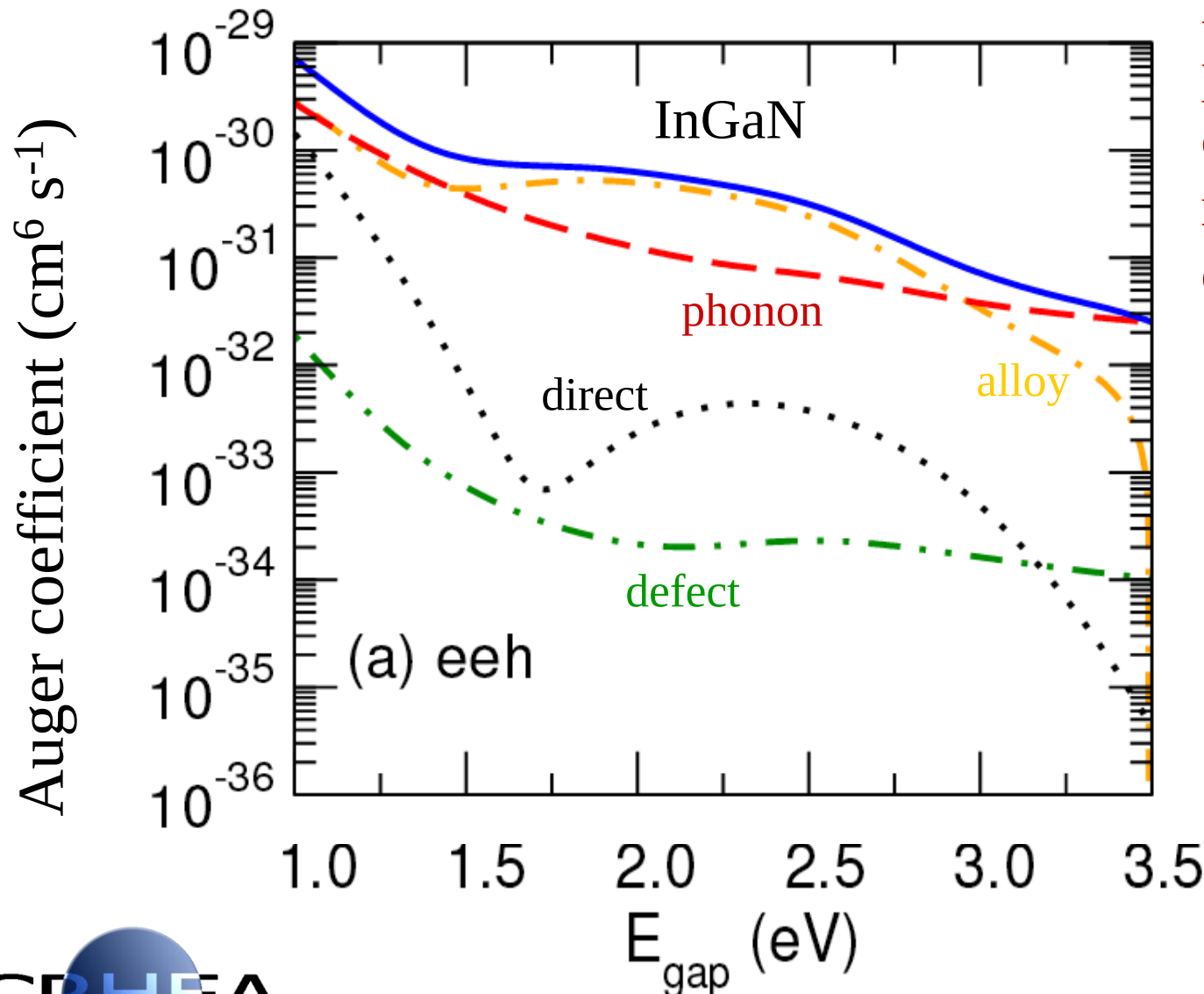
Auger



The Auger coefficient does not decrease with band gap above 1.4 eV (wide band gap are similar to normal band gap materials. Why ?)

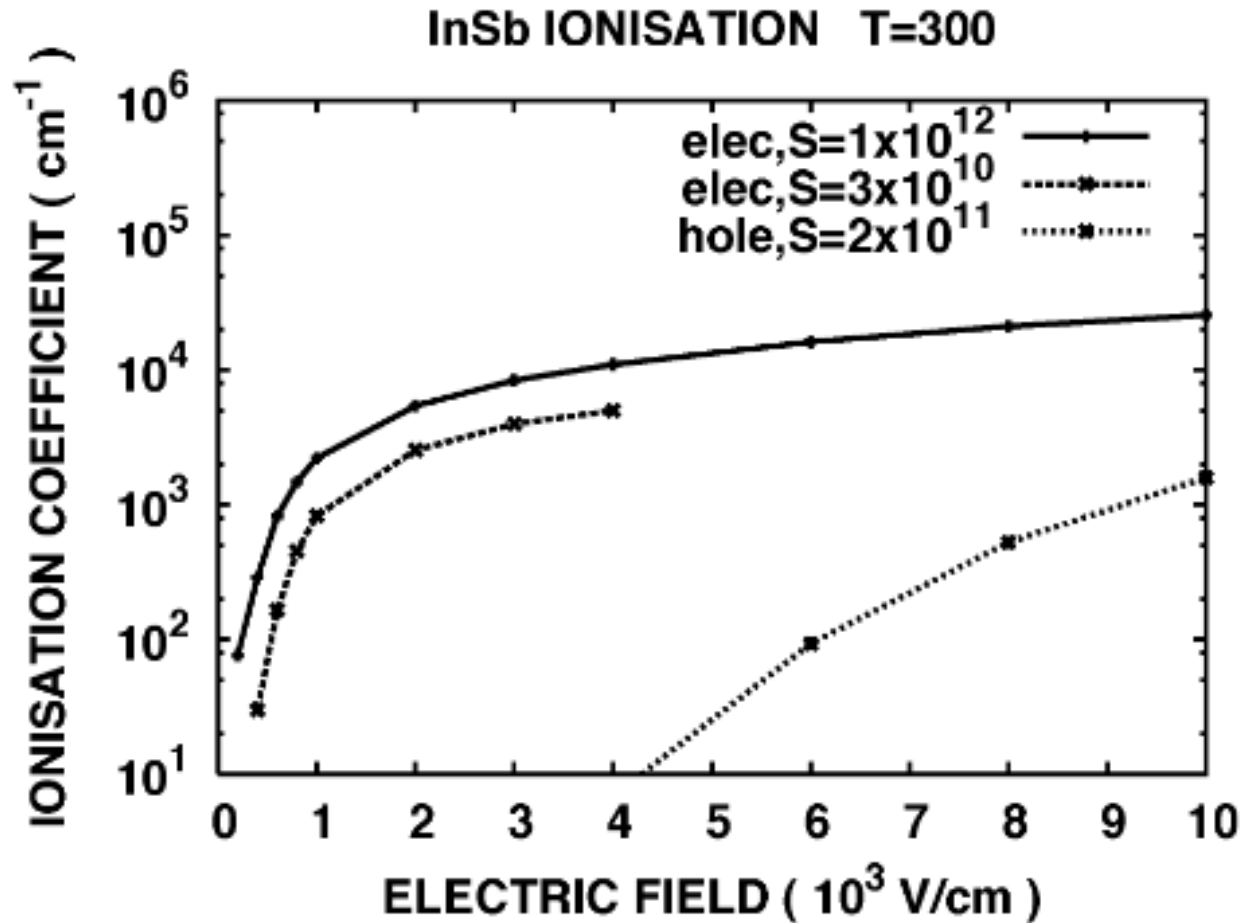
Auger

Extrinsic Auger mediated by phonons, etc...which relaxes the E-k conservation rule



Ionisation coefficient

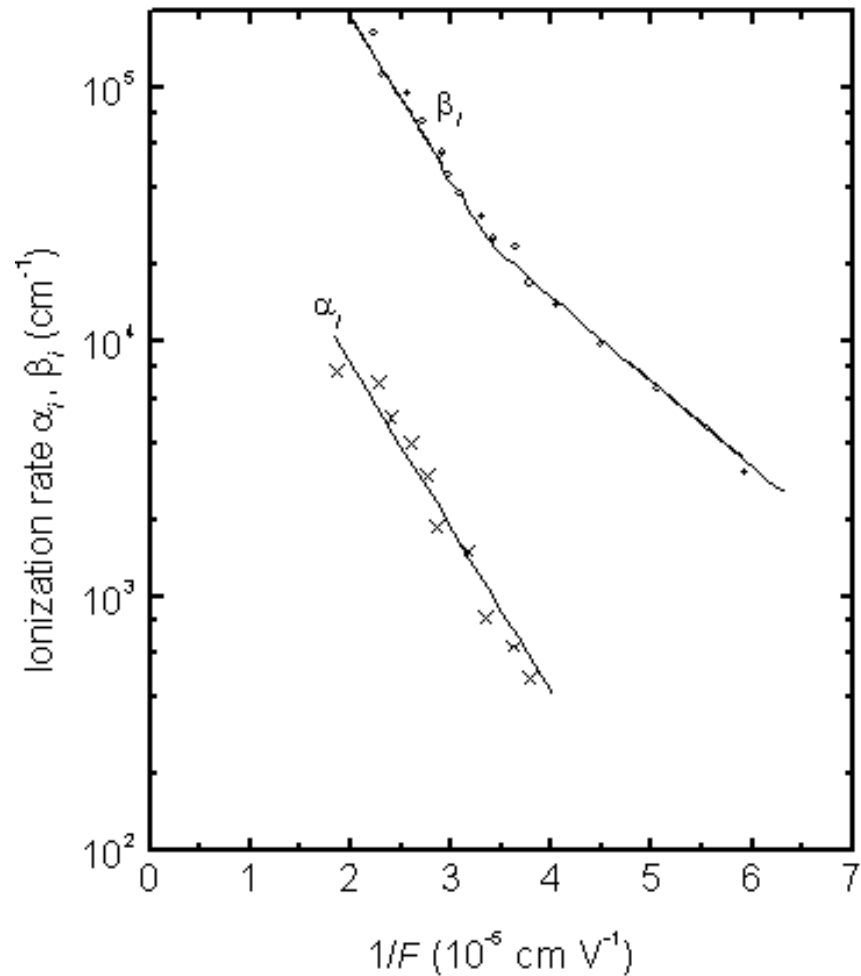
InSb $E_g=0.17$ eV



Ionisation coefficient

InAs

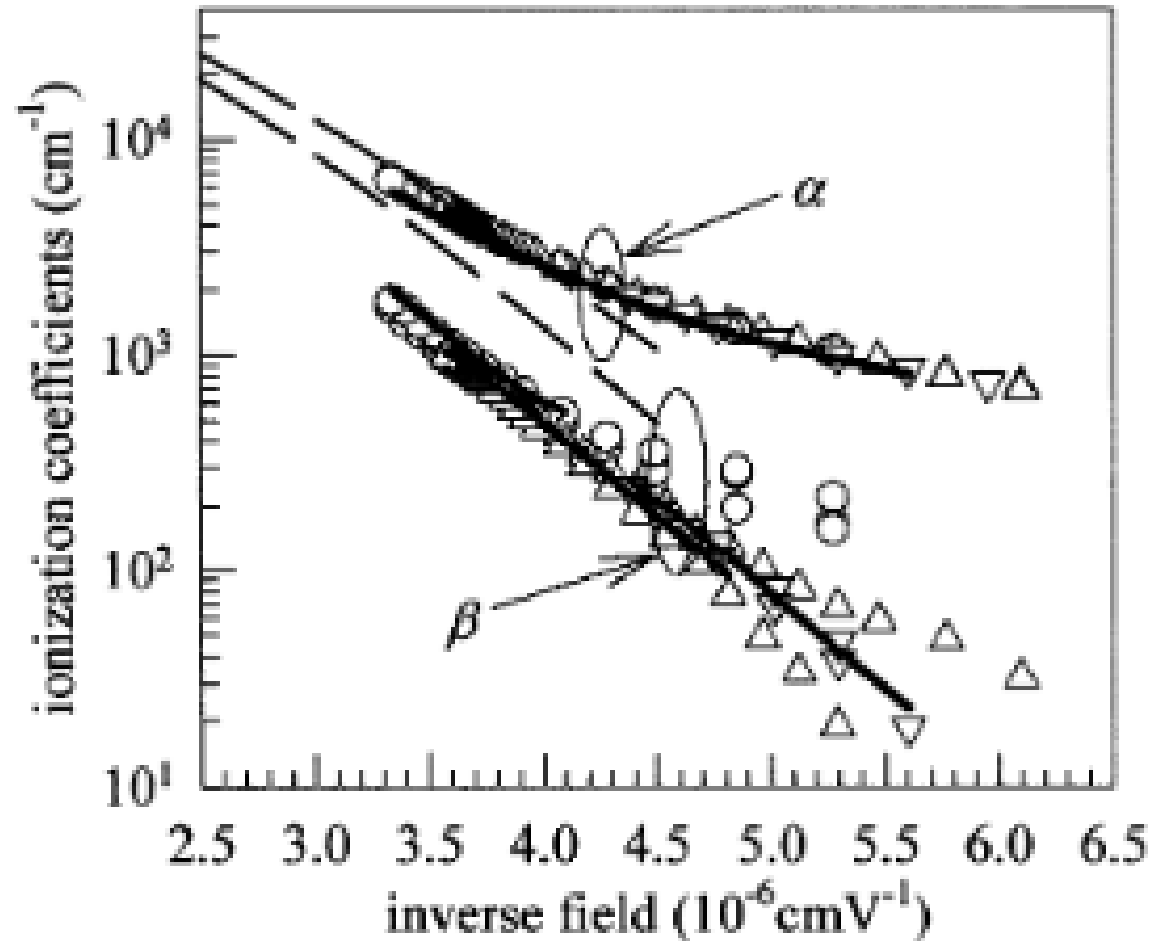
$E_g = 0.35$ eV



Ionisation coefficient

$\text{In}_{0.53}\text{Ga}_{0.47}\text{As}$

$E_g = 0.8 \text{ eV}$

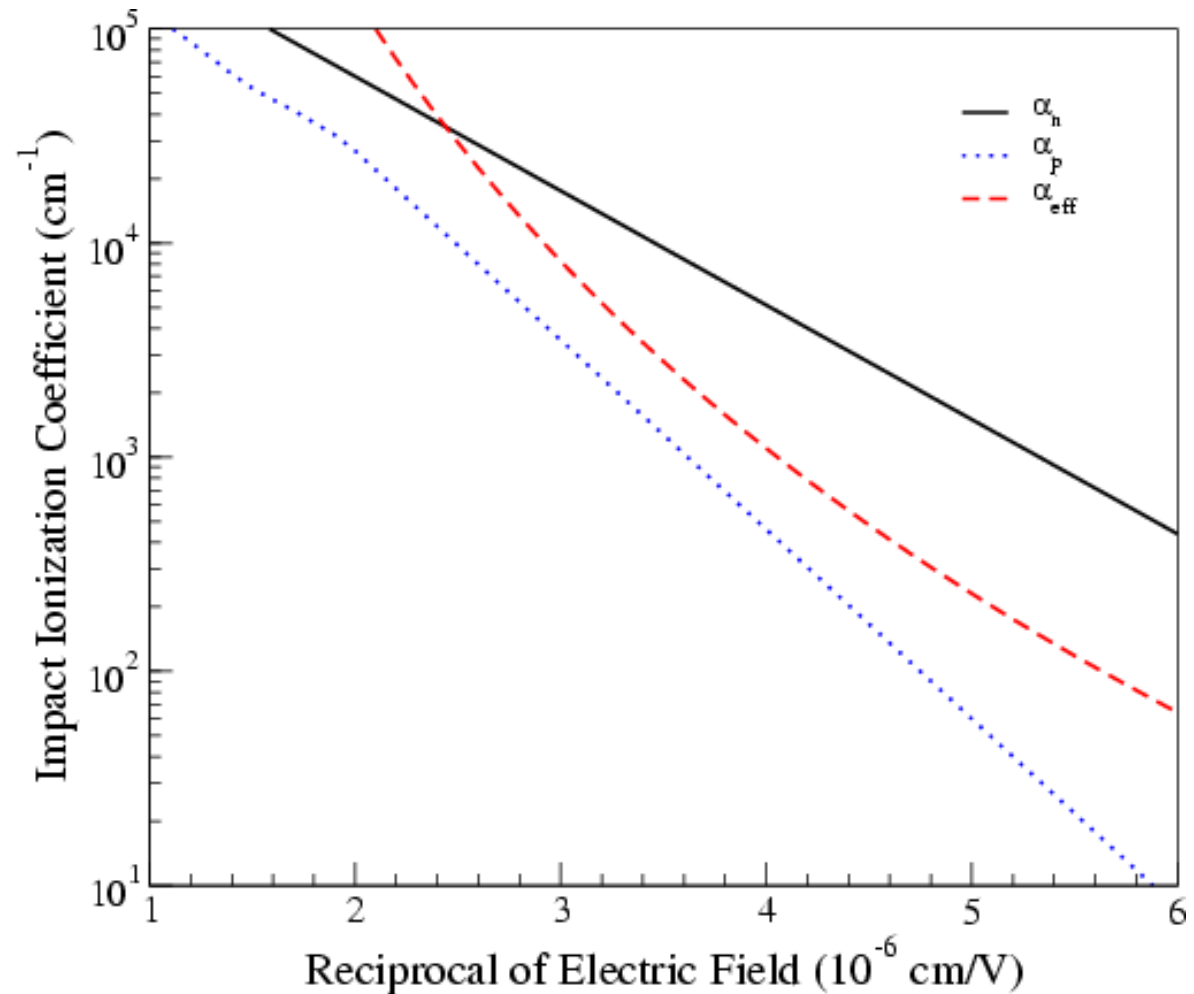


S. Ng et al, Field Dependence
of Impact Ionization Coefficients
in $\text{In}_{0.53}\text{Ga}_{0.47}\text{As}$. S. Ng
IEEE TRANSACTIONS ON
ELECTRON DEVICES, VOL.
50, NO. 4, APRIL 2003

Ionisation coefficient

Si

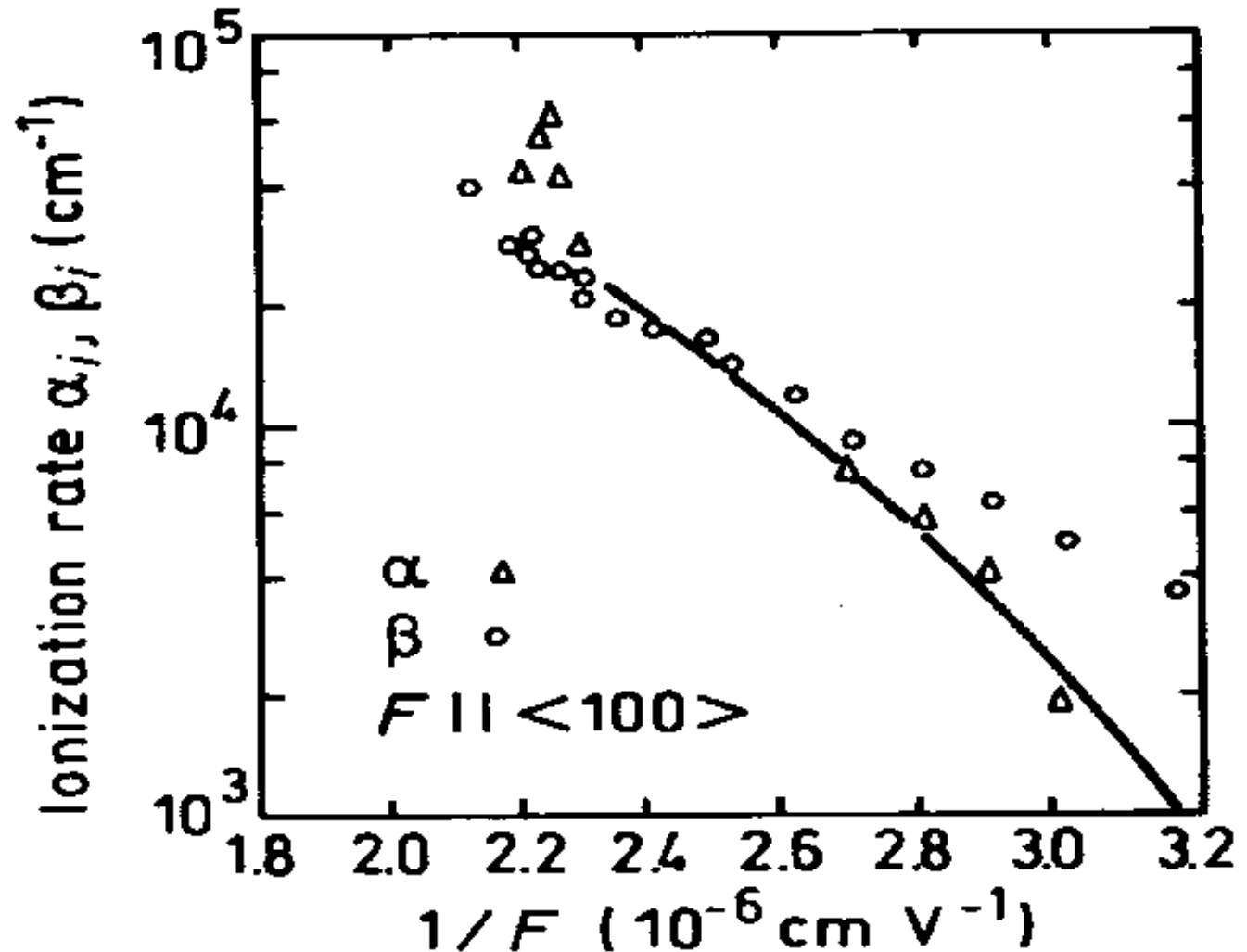
$E_g = 1.11$ eV



Ionisation coefficient

GaAs

$E_g = 1.41$ eV

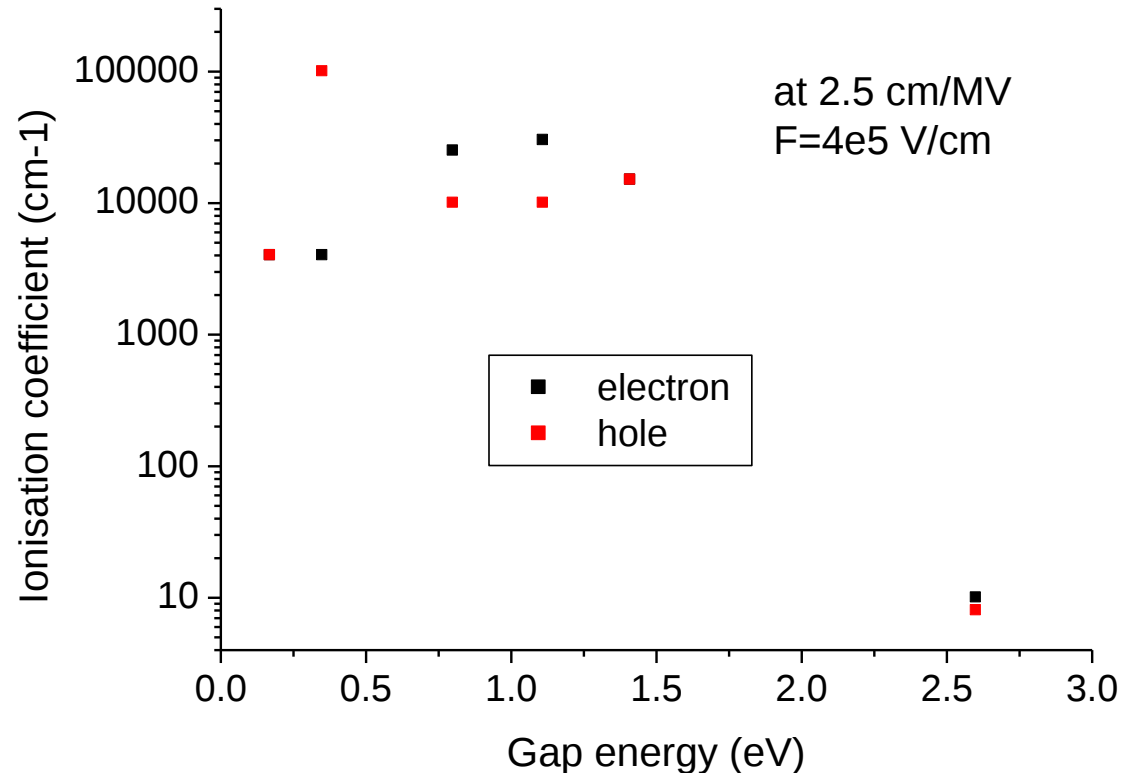


Pearsall, T. P., F.
Capasso, R. E.
Nahory, M. A. Pallack,
and J. Chelikowsky,
Solid State Electron.
21, 1 (1978) 297-302

Ionisation coefficient

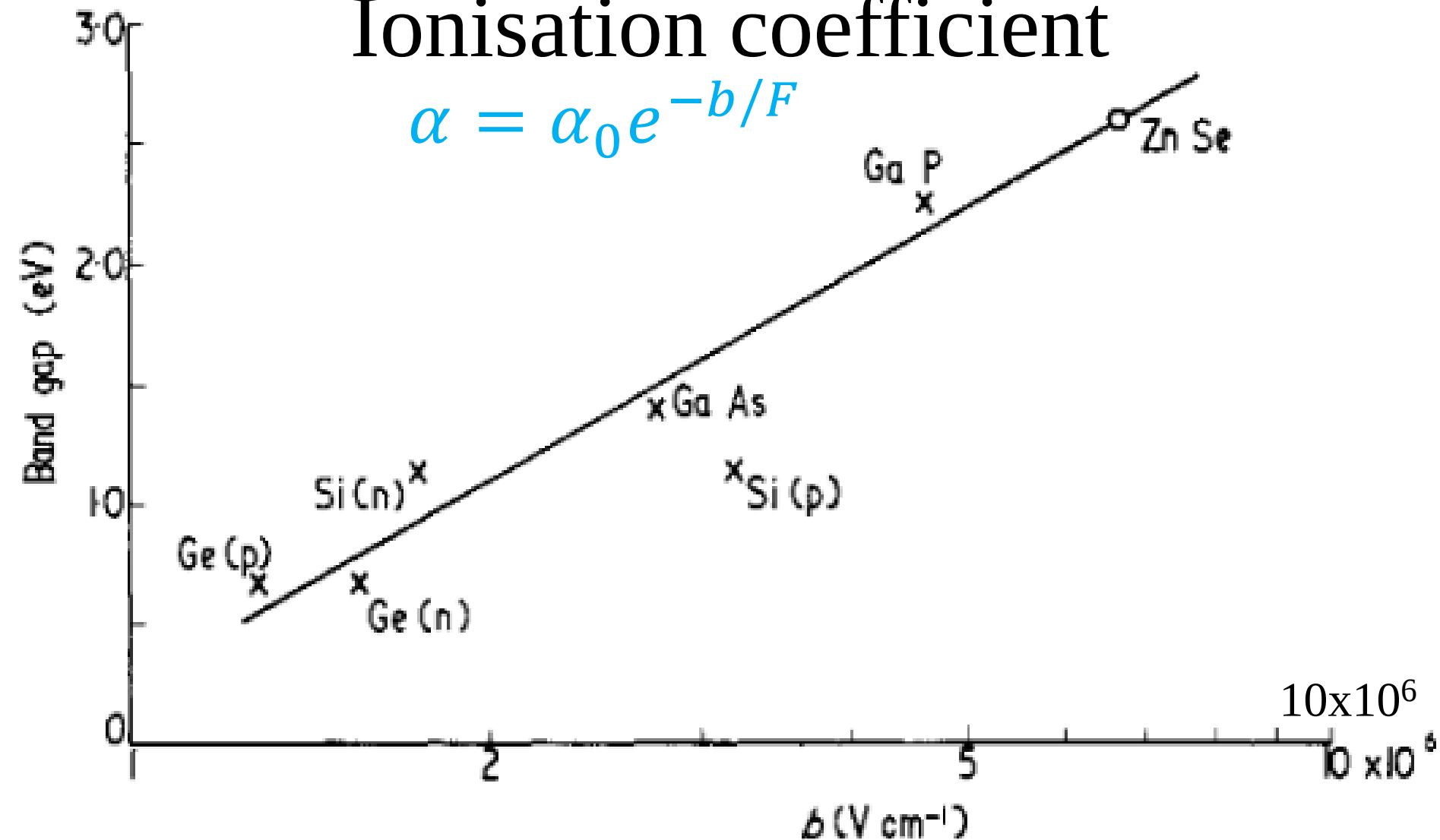
At high field, all material have similar ionisation coefficients (saturation)

Only ZnSe is not saturated at $4e5 \text{ V/cm}$

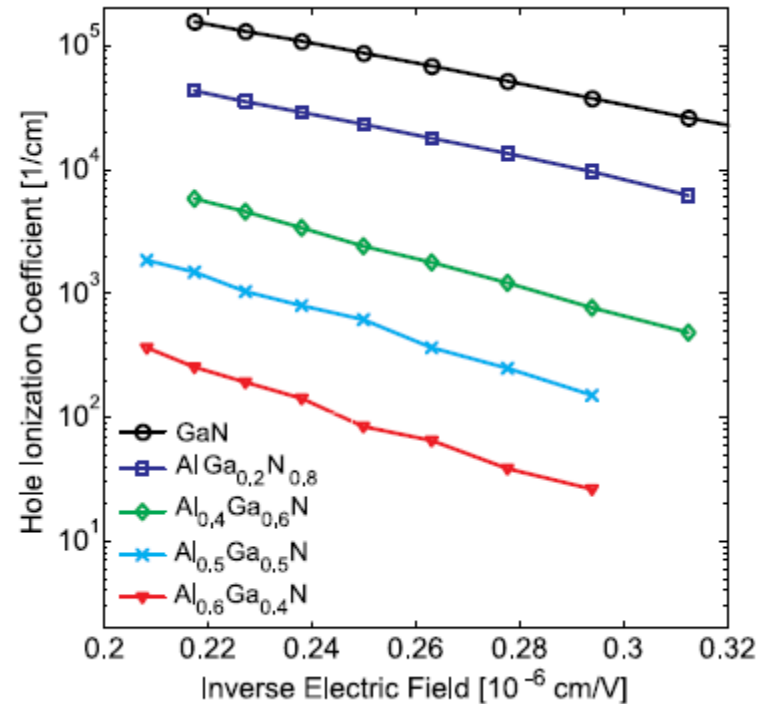
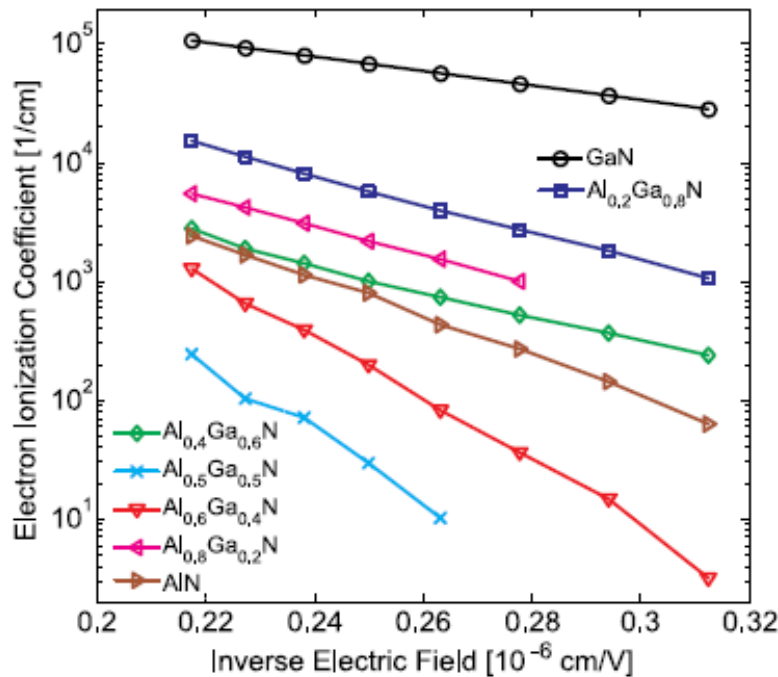


Ionisation coefficient

$$\alpha = \alpha_0 e^{-b/F}$$



Ionisation coefficient

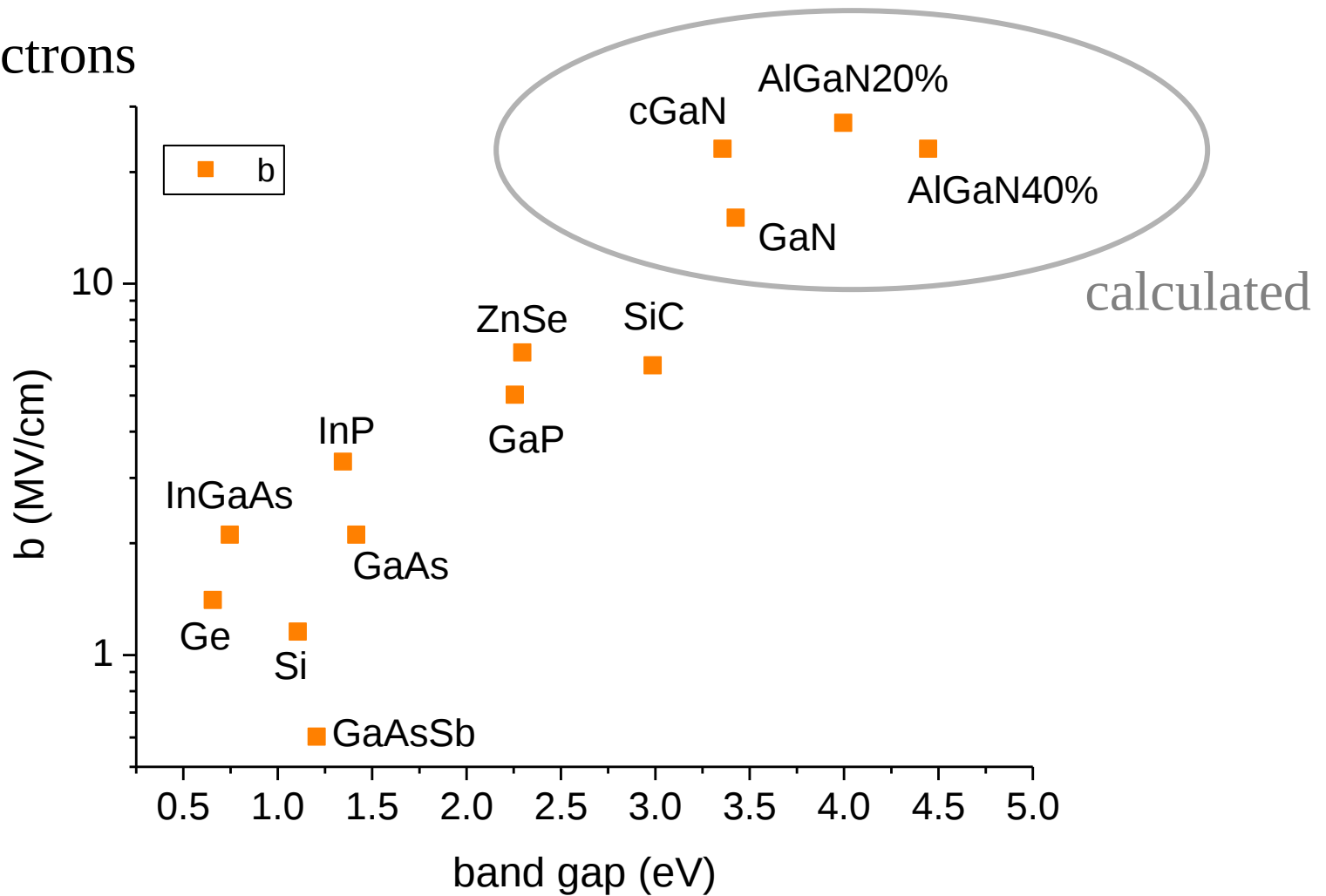


Calculated ionisation rates very weak in nitrides

Phonon assisted ionization not included (may be important in the k conservation; also phonon interaction strong in nitrides)

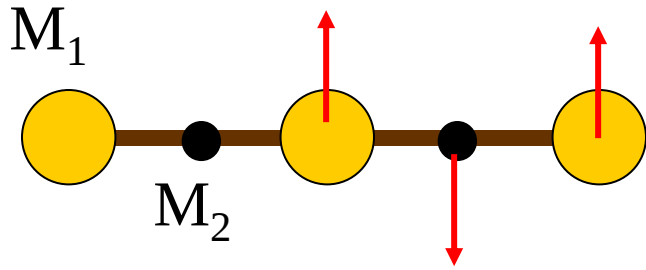
Ionisation coefficient

For electrons

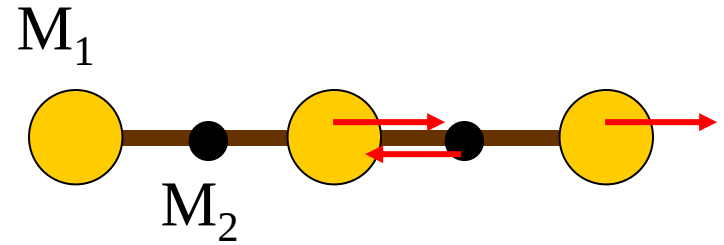


All materials reach similar ionization coefficients, but not for the same fields ! Nitrides have larger breakdown fields than many other SCs

Phonons



TO- Transverse optic

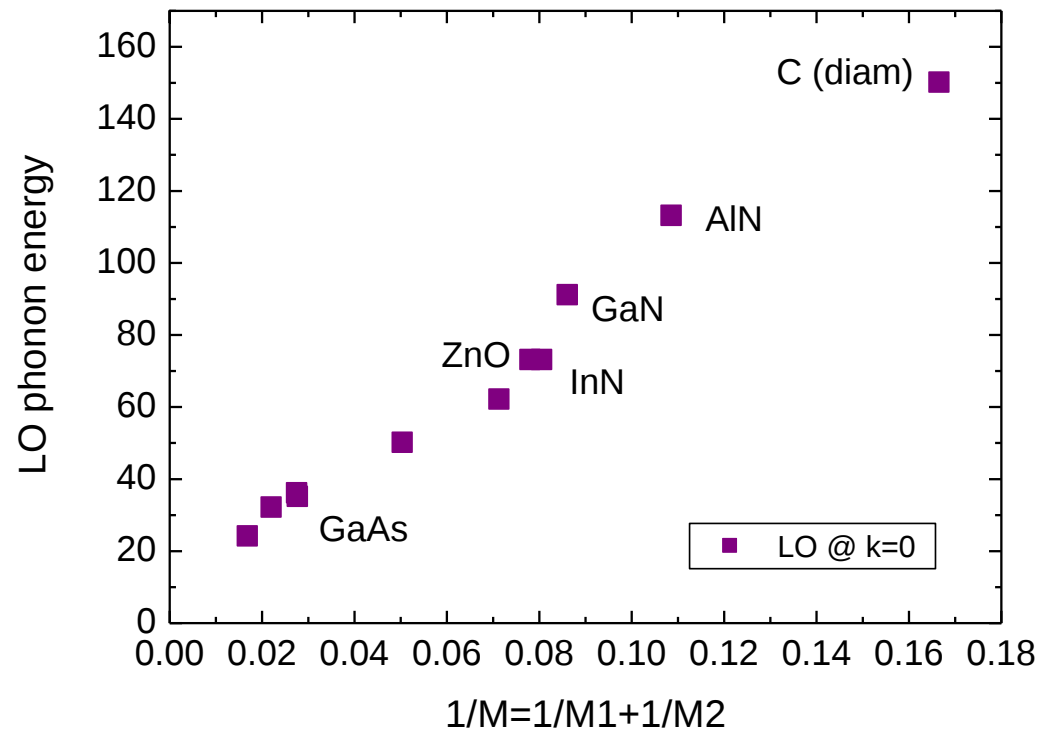


LO- Longitudinal optic

Simple model:

$$\omega^2 = \frac{2C}{M}$$

$$\frac{1}{M} = \frac{1}{M_1} + \frac{1}{M_2}$$



M is small in nitrides $\Rightarrow \omega$ is large

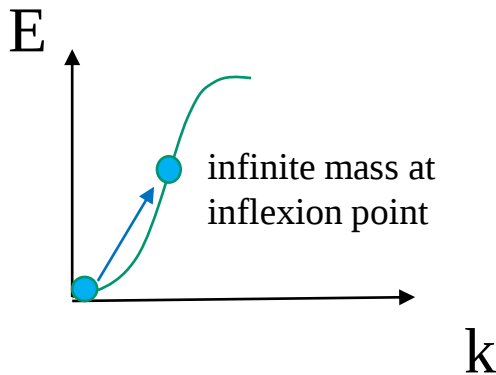
$E_{LO} = 91$ meV, $E_{TO} = 70$ meV in GaN

Saturation velocities

$$\hbar d\mathbf{k} = F dt$$

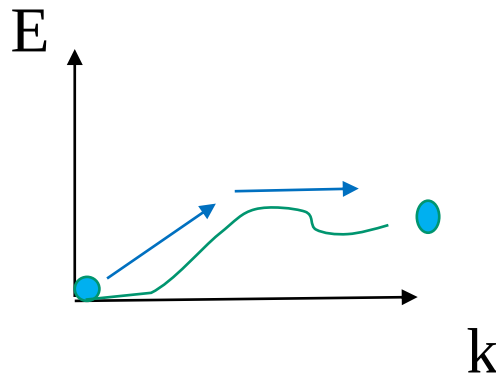
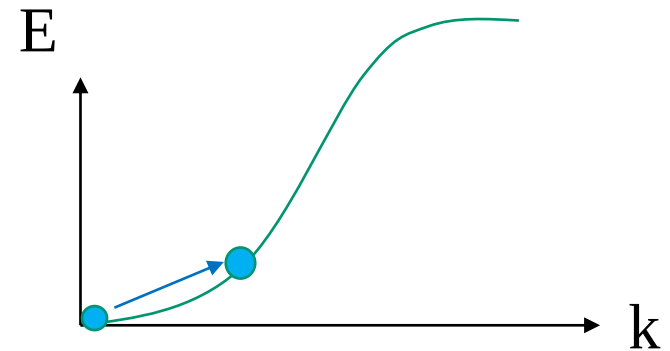
$$v_g = \frac{1}{\hbar} \nabla_k E$$

GaAs

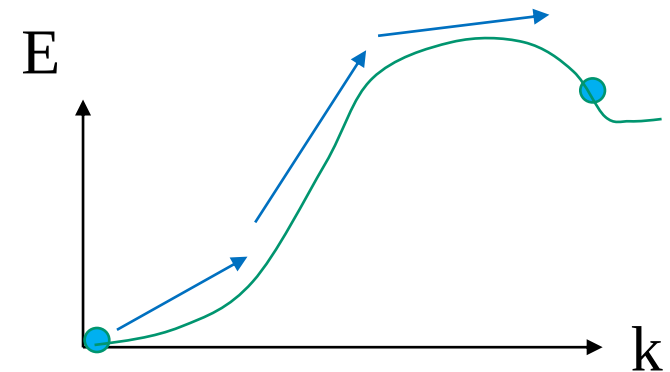


Non
parabolicity,
band
curvature

GaN



valley
transfer

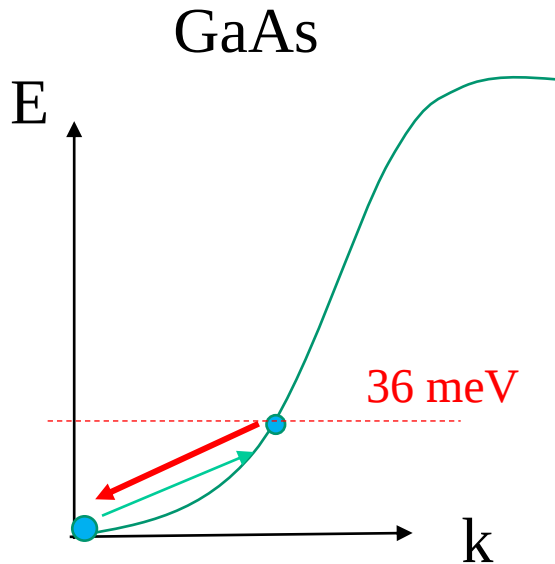


Velocity saturation is reached for higher fields in nitrides

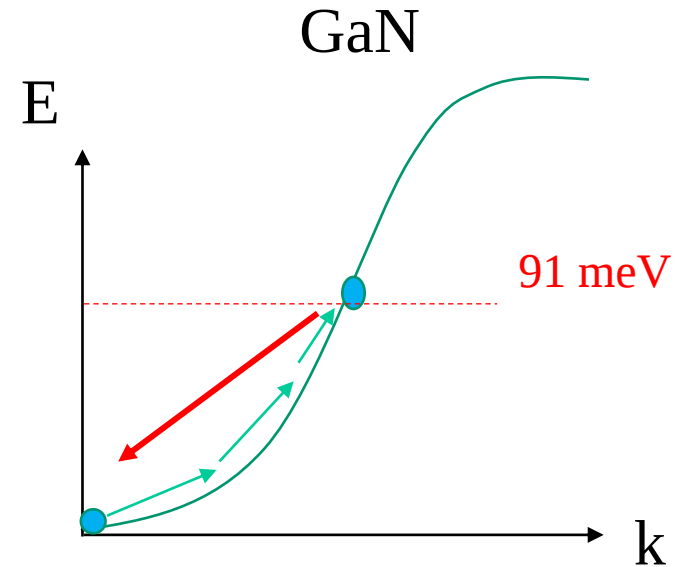


Saturation velocities

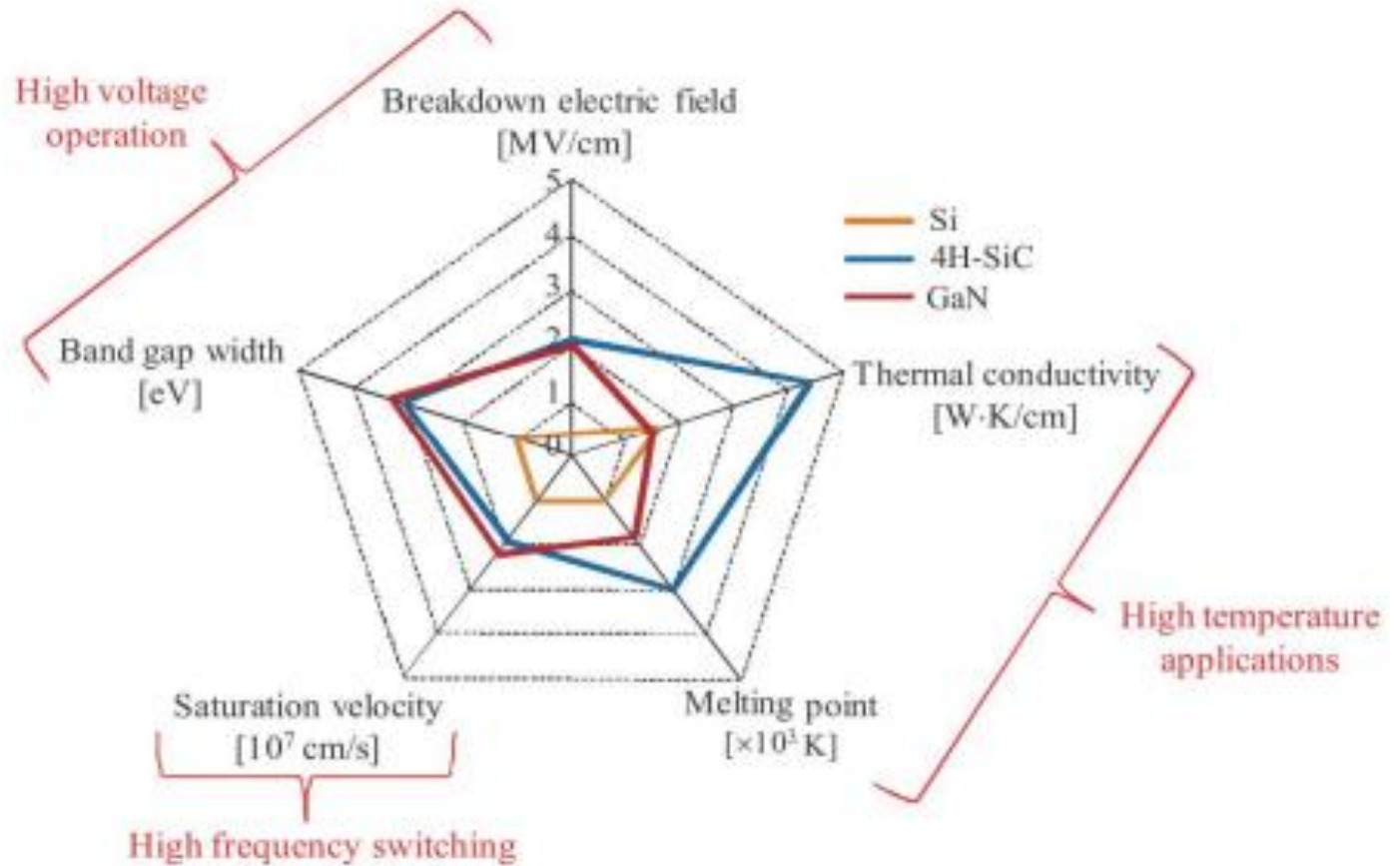
$$\hbar dk = F dt$$



LO
phonon
emission



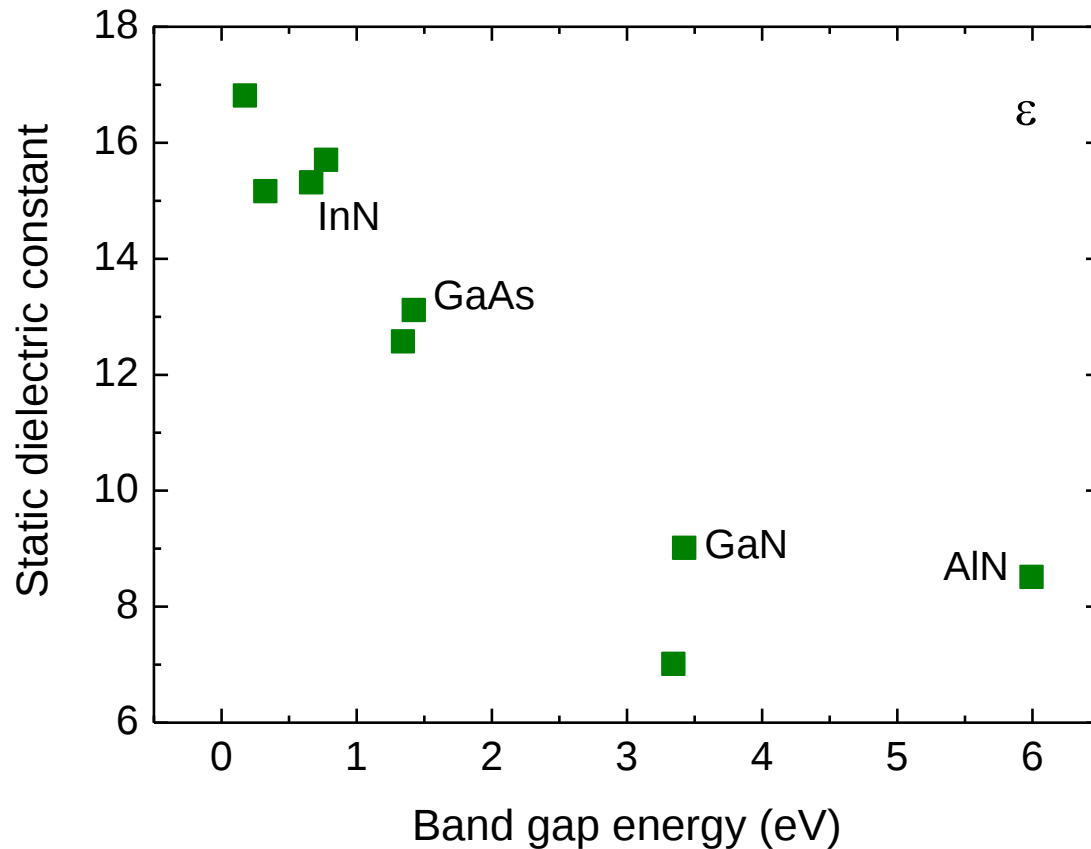
Semiconductors for electronics



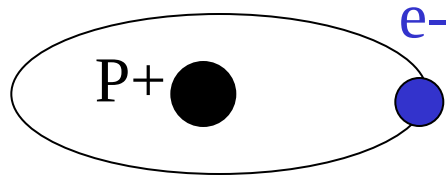
Static dielectric constant

Shorter bonds, less polarizable by a constant external field :

⇒ small dielectric constant



Hydrogenoid model

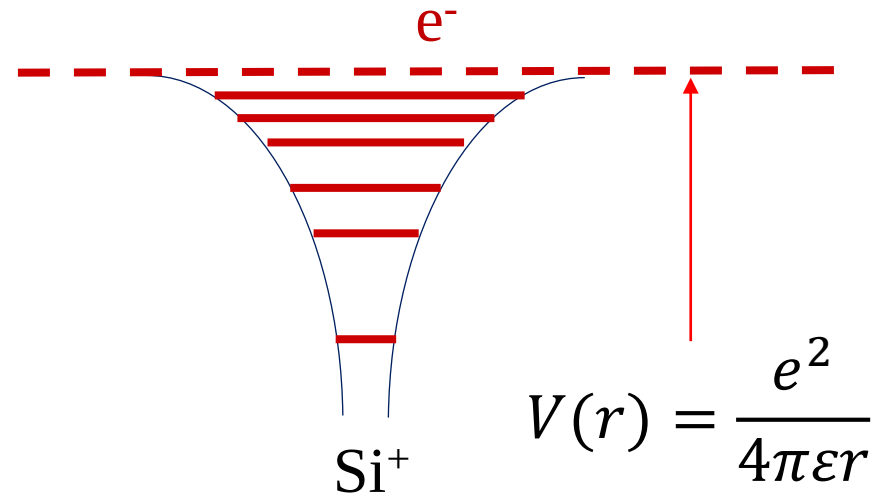


$$1/\mu = 1/m_e + 1/m_p$$

$$E = \frac{\mu e^4}{32\pi^2 \hbar^2 \epsilon^2} = \frac{\mu}{m_0} \frac{1}{\epsilon_r^2} R_y$$

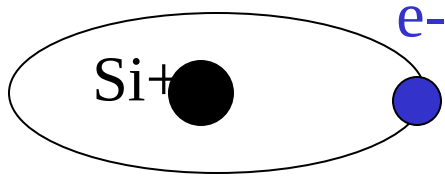
with $R_y = 13.6 \text{ eV}$

Static relative dielectric constant



NB: Hydrogenoid model accurate only for large Bohr radii ($r > 2 \times \text{cell}$) i.e. small energies ($E < 50 \text{ meV}$)

Donors



$$E = \frac{m_e}{m_0} \frac{1}{\epsilon_r^2} R_y$$

Large donor energies are expected in nitrides (37 meV)

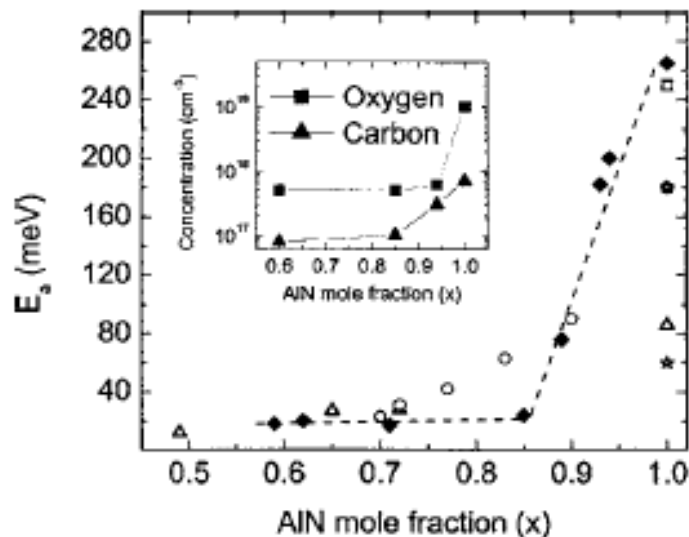
$$1/\mu = 1/m_e + 1/m_{Si} \approx 1/m_e$$

O : shallow donor in GaN (26 meV) but deep level in AlGaN

Si: shallow donor in GaN (25 meV), deeper in AlGaN

	GaAs	GaN	AlAs	AlN
E_{Si} measured (meV)	5.8	25	70	250/60

B. Borisov, APL 87,132106 (2005)

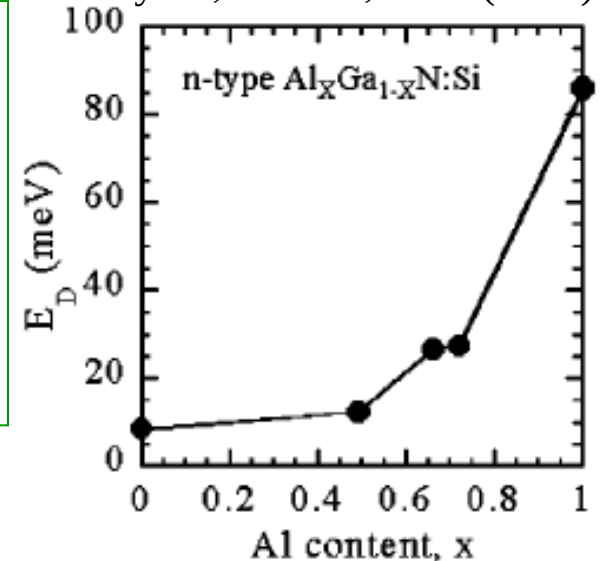


Donor energy renormalized at high concentration

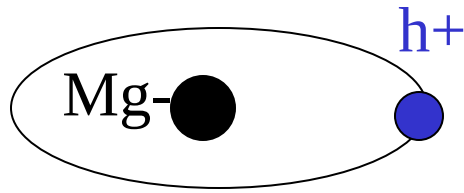
$$E = E_0 - \beta n^{1/3}$$

$$\beta = 10^{-8} \text{ eV/cm}$$

Taniyasu, APL 81, 1255 (2002)



Acceptors



$$E = \frac{m_e}{m_0} \frac{1}{\epsilon_r^2} R_y$$

Very large acceptor energies are expected in nitrides (168 meV with $m_h=1$): not hydrogenoid !

$$1/\mu = 1/m_h + 1/m_{Mg} \approx 1/m_h$$

$$E_{Mg} = 220 \text{ meV}$$

$\Rightarrow$ Low ionization ratio

$\Rightarrow$ Large Mg densities necessary: $5 \times 10^{19} \text{ cm}^{-3}$ for $p = 5 \times 10^{17} \text{ cm}^{-3}$

Doping in semiconductors

	GaN	SiC	ZnO	Diamond	GaAs	Si
n-type dopant	Si on Ga site (~ 15 meV)	N on C site (~ 85 meV)	B on Zn (~30-60 meV)	N (~ 1.7 eV)	Si 6meV	P 45meV
p-type dopant	Mg on Ga site (160 meV) Zn ~ 340 meV	Al on Si site (~ 200 meV)	N on O site (~ 170-200 meV)	B (~ 370 meV)	C (Be) ~28 meV	B 40meV
n-conductivity*	~ 0.002 Ωcm	~ 0.01 Ωcm	~ 0.02 Ωcm	> 1000 Ωcm	~ 0.001 Ωcm	
p-conductivity*	0.2-2 Ωcm	0.5-2 Ωcm	0.5-40 Ωcm	10-100 Ωcm		

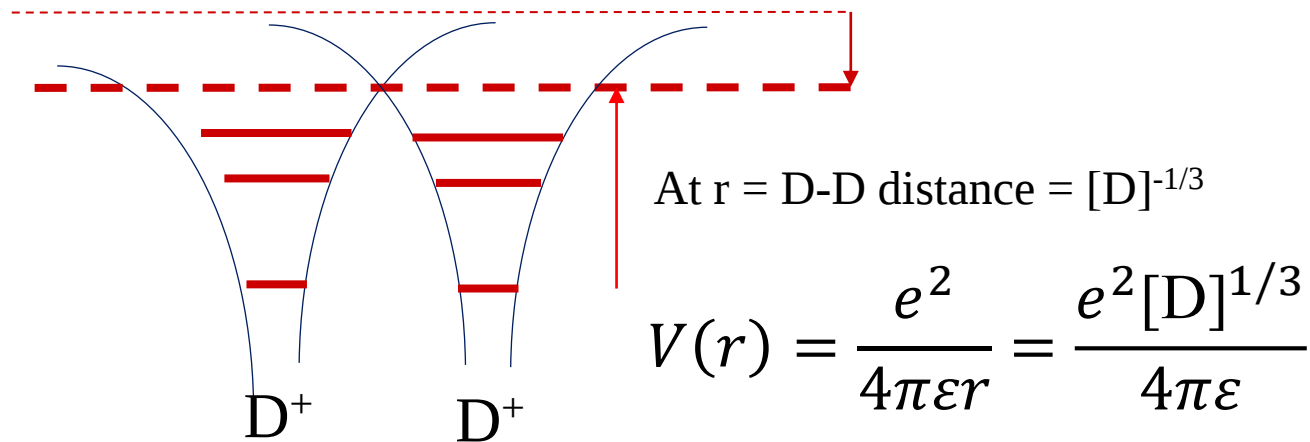
* Experimental values

Variation of donor and acceptor
energy among samples, with
doping.

Renormalization, screening...of
the binding energy ?

What are we talking about ?

Activation energy of donors



E_D is decreased by $\beta[D]^{1/3}$ with

$$\beta = \frac{e^2}{4\pi\epsilon} = 1.6 \times 10^{-8} \text{ eVcm}$$

Rigorous calculation should include the shift of the 1s state but finally leads to the same result !

Experiments:

$\beta = 1.6 \times 10^{-8} \text{ eVcm}$ on Ge [A Ajay *et al* 2016 *J. Phys. D: Appl. Phys.* **49** 445301],
 $\beta = 2 \times 10^{-8} \text{ eVcm}$ on Si [B. Meyer *et al*, *Solid State Com*, 95, 9, 597-600 (1995)]

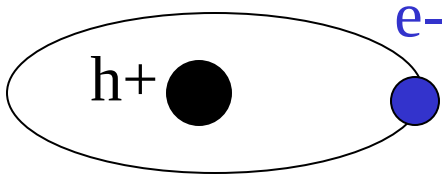
Examples:

GaN: $[\text{Si}] = 3 \times 10^{17} \text{ cm}^{-3}$, $E_D = 25 - 1.6 \times 10^{-5} \times (3 \times 10^{17})^{1/3} = 25 - 11 = 14 \text{ meV}$

$\text{Al}_{0.7}\text{Ga}_{0.3}\text{N}$, $[\text{Si}] = 5 \times 10^{19} \text{ cm}^{-3}$, $E_D = 60 - 1.6 \times 10^{-5} \times (5 \times 10^{19})^{1/3} = 60 - 58 = 2 \text{ meV}$

When $E_D = 0$, Mott transition towards metallic behavior

Excitons



$$1/\mu = 1/m_e + 1/m_h$$

$$E = \frac{\mu}{m_0} \frac{1}{\epsilon_r^2} R_y = 30 \text{ meV} \quad \text{expected}$$

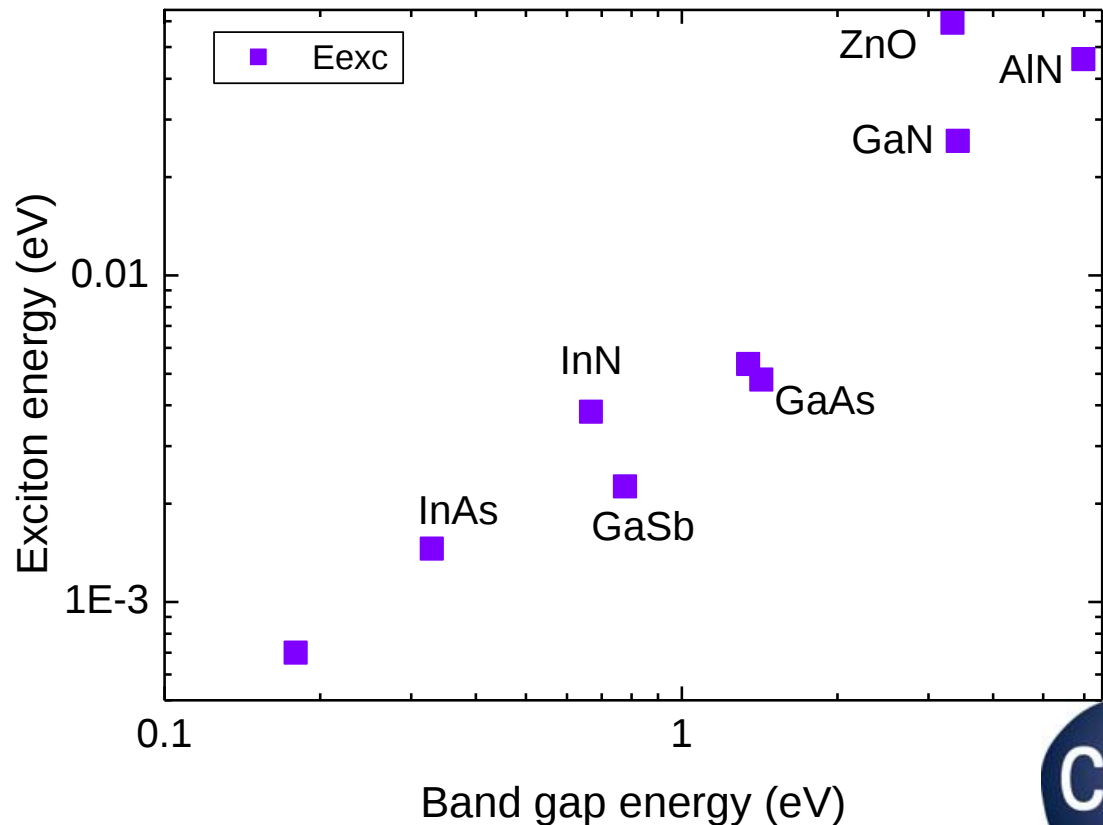
$$E = \frac{\mu}{m_0} \frac{1}{\epsilon_r^2} R_y$$

$$E \propto \frac{E_{\text{gap}}}{\epsilon_r^2}$$

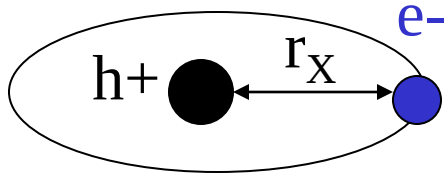
$$E \propto (E_{\text{Gap}})^n$$

with $n > 1$

Decreases
with gap



Excitons



$$E_x (\text{GaN}) = 26 \text{ meV} \approx kT @ 300\text{K}$$

$\Rightarrow$ Exciton stable at room temperature

$$E = \frac{e^2}{8\pi\epsilon r_X}$$

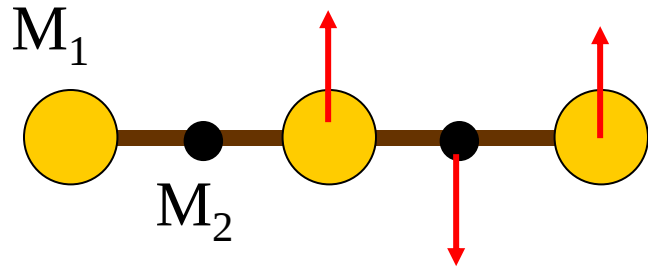
$$r_X = r_{\text{Hydro}} \frac{m}{\mu} \epsilon_r^2$$

r_X small $\Rightarrow$ exciton stable at high density

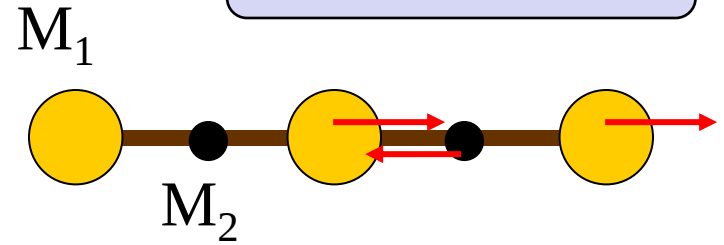
	Bohr radius	Mott density
GaAs	11.6nm	$3\text{-}12 \times 10^{16} \text{ cm}^{-3}$
GaN	2.8nm	$2 \times 10^{18} \text{ cm}^{-3}$

Absorption and emission in nitrides are dominated by excitons (A,B,C)

Phonons



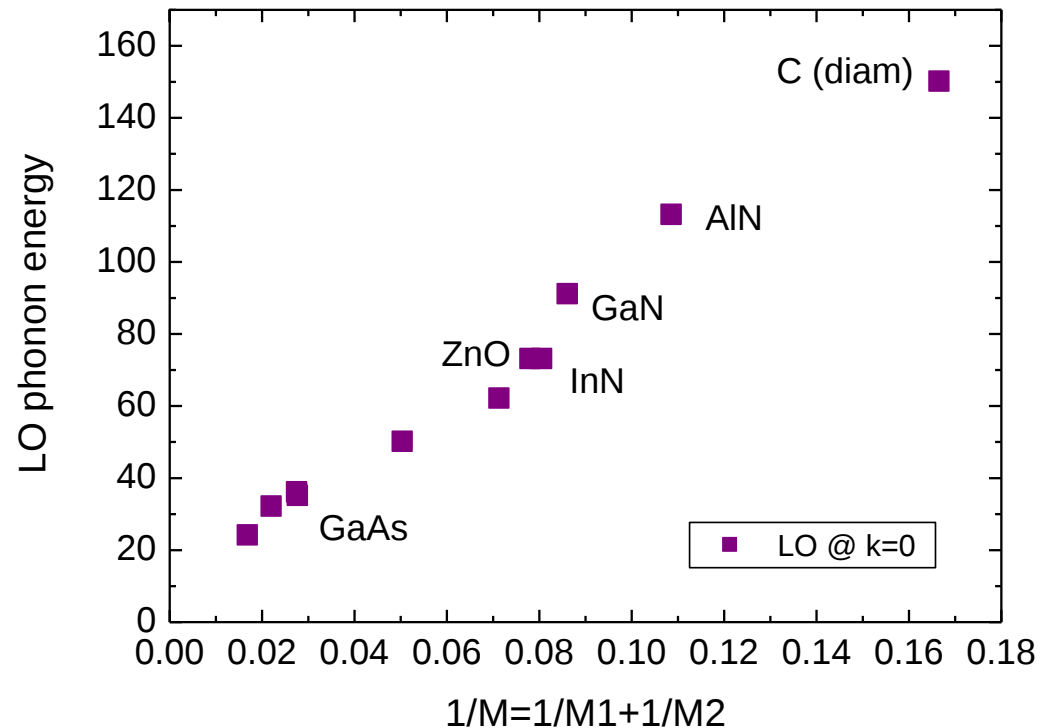
TO- Transverse optic



LO- Longitudinal optic

$$\omega^2 = \frac{2C}{M}$$

$$\frac{1}{M} = \frac{1}{M_1} + \frac{1}{M_2}$$



M is small in nitrides $\Rightarrow \omega$ is large

$E_{LO} = 91$ meV, $E_{TO} = 70$ meV in GaN

Phonons and dielectric constant

$$\omega_{LO} = 91 \text{ meV}$$

$$\omega_{TO} = 70 \text{ meV}$$

$$\left(\frac{\omega_{LO}}{\omega_{TO}}\right)^2 = 1.69$$

$$\epsilon_{static} = 9$$

$$\epsilon_{\infty} = n^2 = 2.3^2$$

$$\frac{\epsilon_{static}}{\epsilon_{\infty}} = 1.69$$

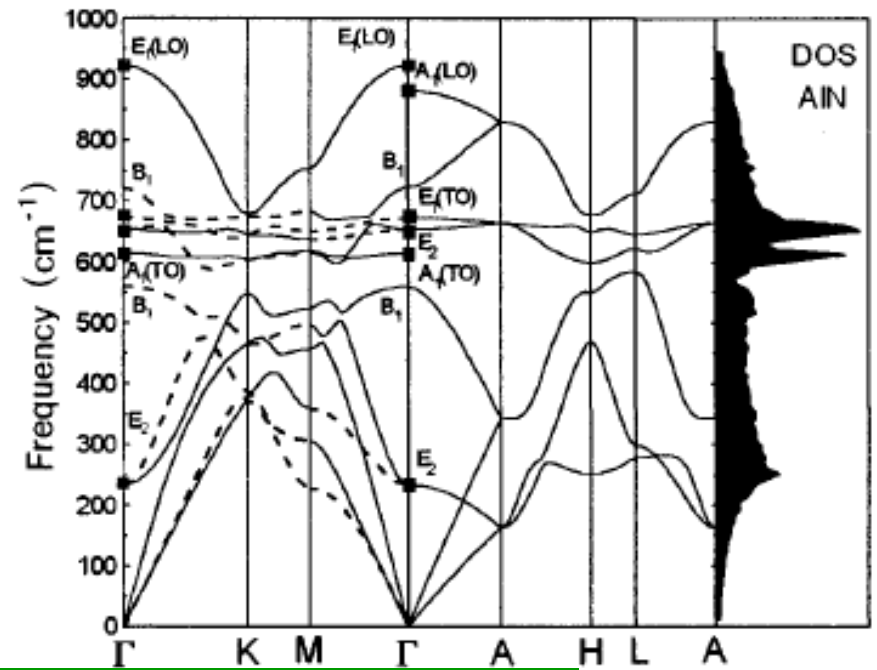
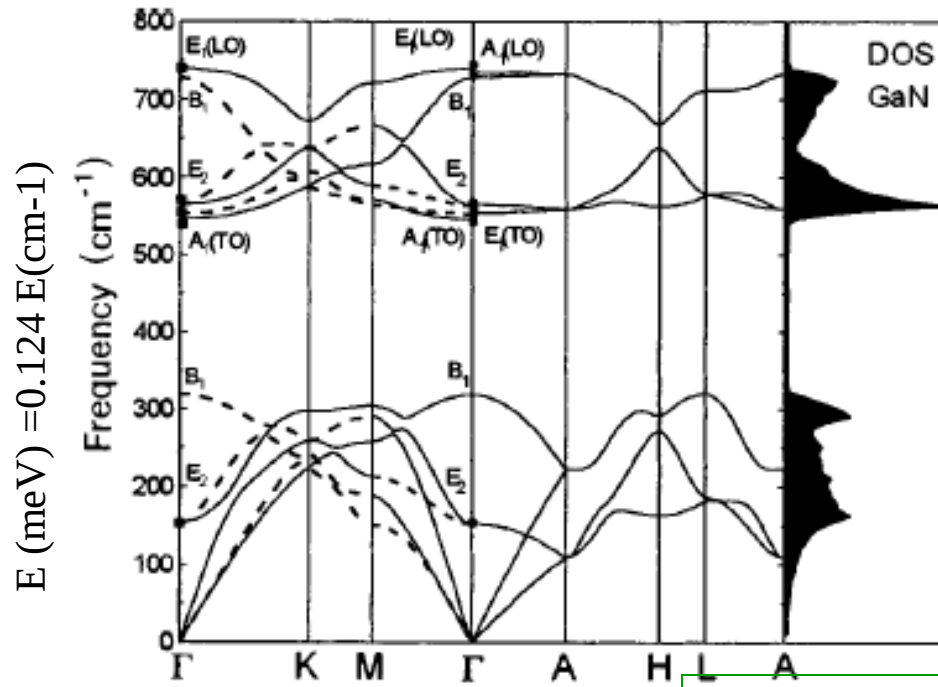
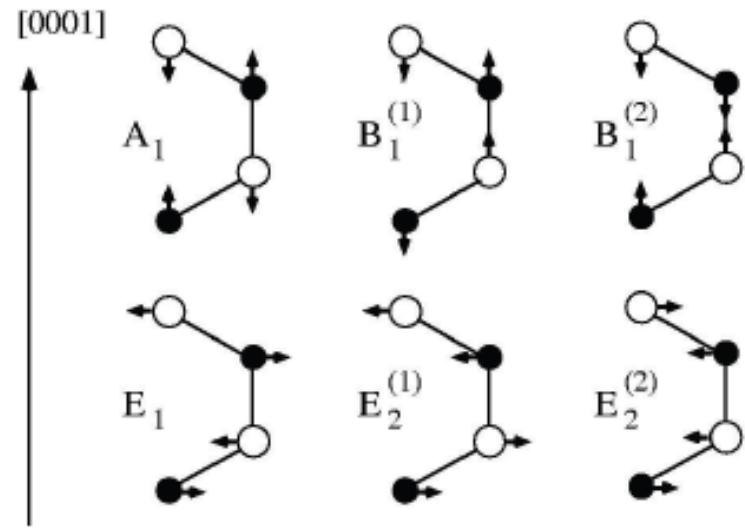
What is the difference between ϵ_{static} and ϵ_{∞} ?

What a nice coincidence !!!!??

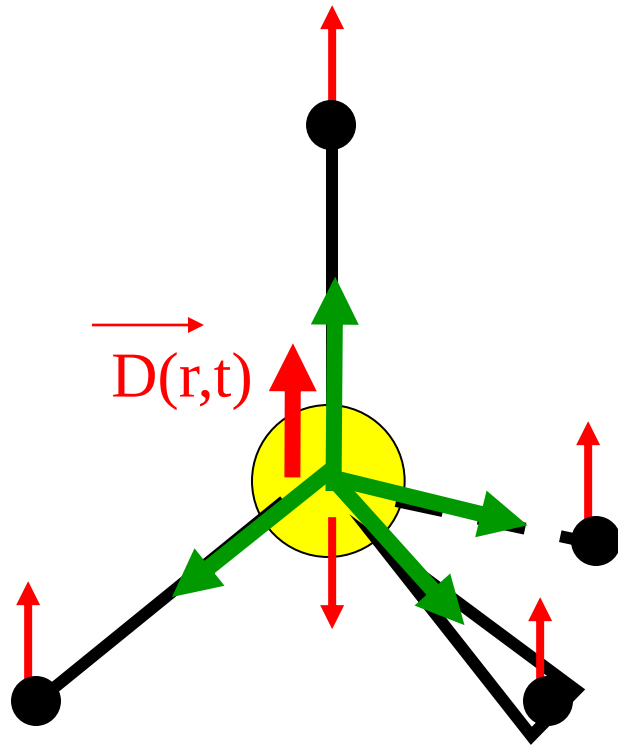
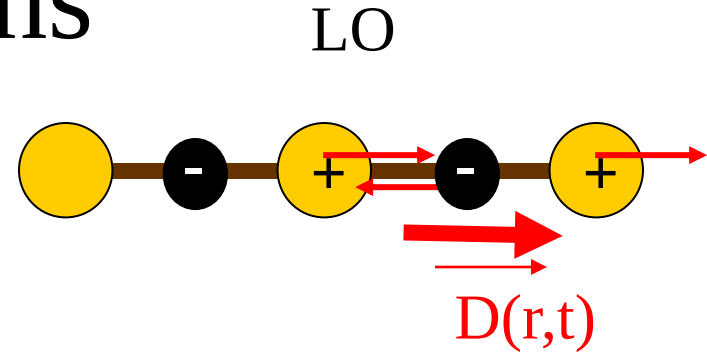
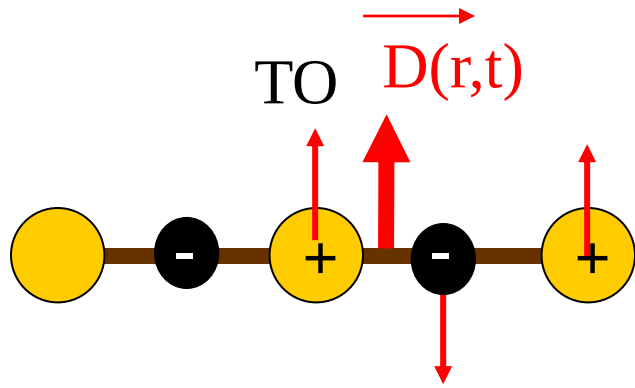
Lyddane–Sachs–Teller relation

$$\left(\frac{\omega_{LO}}{\omega_{TO}}\right)^2 = \frac{\epsilon_{static}}{\epsilon_{\infty}}$$

Phonons



Phonons



Polar atomic bond $\Rightarrow$ phonons are associated with an electric polarization $\Rightarrow$ strong coupling with electrons

Pure TO do not couple with electrons *, however mixt TO-LO in nitrides couple (but coupling 10^3 smaller than for LO)

τ_{e-LO} GaN = 1/10 τ_{e-LO} GaAs = a few 10 fs

Summary

Most nitride properties can be estimated by rules of thumb or an educated guess, and compared with those of other SCs

- Wide band gap energy and large band offsets
- Chemical inertness and thermal stability
- Large effective masses
- Low mobilities and large saturation velocities
- Excitonic effects and large oscillator strengths
- Ionic bonds and large internal fields
- Deep donors and acceptors
- High energy optical phonons strongly coupled with charged carriers